

การเปลี่ยนแปลงลักษณะฐานท้องน้ำแบบตะกอนทราย
ภายใต้การไหลแบบไม่คงที่

MORPHODYNAMIC OF SAND BED EVOLUTION UNDER UNSTEADY FLOW

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KMUTT, Thailand

Outlines

1. Introduction

2. Governing Equations

3. CIP Method

4. Calibration & Application

5. Conclusion



Alatna River, Alaska

(<http://www.terraviva.com>)

1. Introduction

Alatna River, Alaska

(<http://www.ferragallria.com>)

SAND BED RIVER





Image © 2006 DigitalGlobe
Image © 2006 TerraMetrics

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Ping River, Thailand

Pointer 15°54'25.22" N 99°59'39.77" E elev 129 ft

Streaming ||||| 100%

Eye alt 39083 ft



Kok River, Thailand

2. Governing Equation

Alatna River, Alaska

(<http://www.ferragallria.com>)

Continuity eq.

$$\frac{\partial h}{\partial t} + \frac{\partial(hu)}{\partial x} + \frac{\partial(hv)}{\partial y} = 0$$

Momentum eq.

$$\frac{\partial(hu)}{\partial t} + \frac{\partial(hu^2)}{\partial x} + \frac{\partial(huv)}{\partial y} = -gh \frac{\partial H}{\partial x} - \frac{\tau_{bx}}{\rho} + \frac{\partial}{\partial x} \left[\nu \frac{\partial(hu)}{\partial x} \right] + \frac{\partial}{\partial y} \left[\nu \frac{\partial(hu)}{\partial y} \right]$$

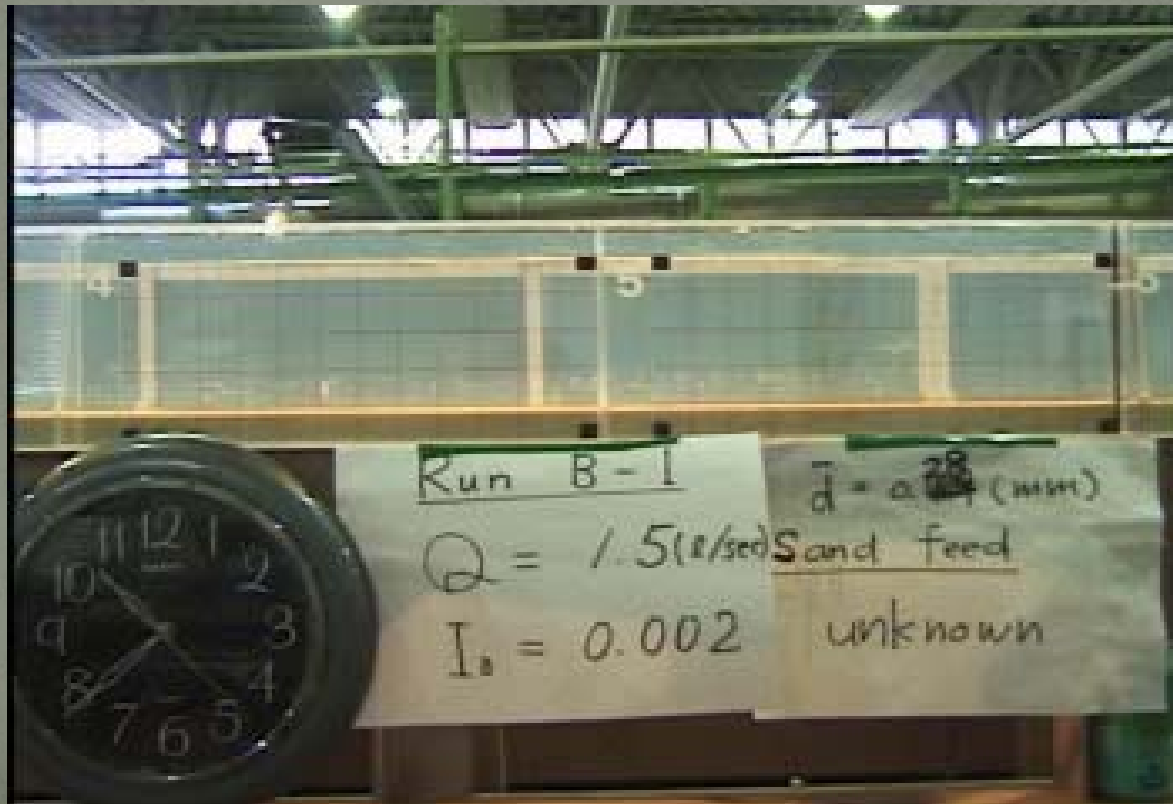
$$\frac{\partial(hv)}{\partial t} + \frac{\partial(huv)}{\partial x} + \frac{\partial(hv^2)}{\partial y} = -gh \frac{\partial H}{\partial y} - \frac{\tau_{by}}{\rho} + \frac{\partial}{\partial x} \left[\nu \frac{\partial(hv)}{\partial x} \right] + \frac{\partial}{\partial y} \left[\nu \frac{\partial(hv)}{\partial y} \right]$$

where h = water depth, u , v = average velocity, τ_b = shear stress, ρ = water density, H = water surface elevation ($=z_b + h$), z_b = bed elevation, ν = eddy viscosity, t = time, and x , y = spatial coordinate in Cartesian coordinate system.

Sediment transport eq.

$$\frac{\partial z_b}{\partial t} + \frac{1}{1-\lambda} \left[\frac{\partial q_{bx}}{\partial x} + \frac{\partial q_{by}}{\partial y} \right] = 0$$

where z_b =bed elevation, λ =porosity of bed material.

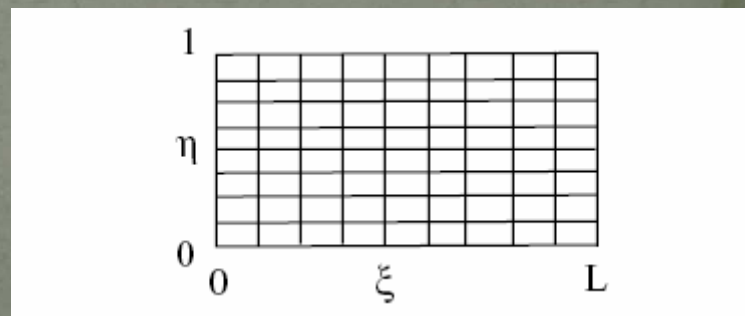
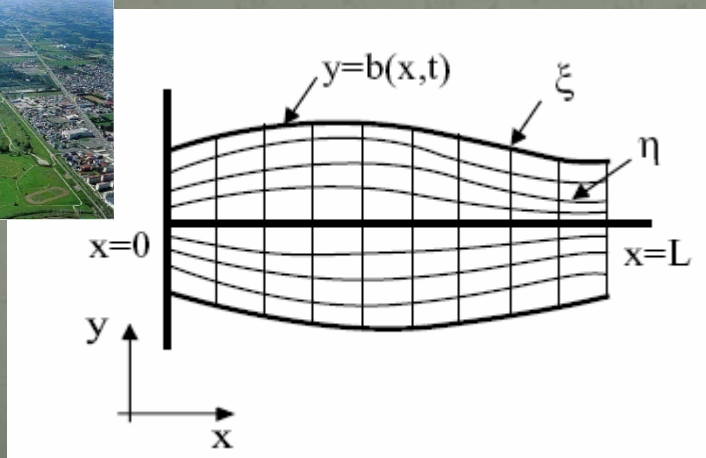


Transformed rule

$$\begin{pmatrix} \frac{\partial}{\partial t} \\ \frac{\partial}{\partial x} \\ \frac{\partial}{\partial y} \end{pmatrix} = \begin{pmatrix} \tau_t & \xi_t & \eta_t \\ \tau_x & \xi_x & \eta_x \\ \tau_y & \xi_y & \eta_y \end{pmatrix} \begin{pmatrix} \frac{\partial}{\partial \tau} \\ \frac{\partial}{\partial \xi} \\ \frac{\partial}{\partial \eta} \end{pmatrix}$$

$$\begin{pmatrix} u \\ v \end{pmatrix} = \frac{1}{J} \begin{pmatrix} \eta_y & -\xi_y \\ -\eta_x & \xi_x \end{pmatrix} \begin{pmatrix} u^\xi \\ v^\eta \end{pmatrix}$$

where u^ξ, v^η = average velocity components in the of ξ, η direction, τ = time, and J = Jacobian of coordinate transformed.



Moving boundary-fitted system

Continuity eq.

$$\frac{\partial}{\partial \tau} \left(\frac{h}{J} \right) + \frac{\partial}{\partial \xi} \left[(\xi_t + u^\xi) \frac{h}{J} \right] + \frac{\partial}{\partial \eta} \left[(\eta_t + u^\eta) \frac{h}{J} \right] = 0$$

Momentum eq.

$$\begin{aligned} & \frac{\partial u^\xi}{\partial \tau} + (\xi_t + u^\xi) \frac{\partial u^\xi}{\partial \xi} + (\eta_t + u^\eta) \frac{\partial u^\xi}{\partial \eta} + \alpha_1 u^\xi u^\xi + \alpha_2 u^\xi u^\eta + \alpha_3 u^\eta u^\eta - D_\xi \\ &= -g \left[(\xi_x^2 + \xi_y^2) \frac{\partial H}{\partial \xi} (\xi_x \eta_x + \xi_y \eta_y) \frac{\partial H}{\partial \eta} \right] - \frac{C_f u^\xi}{hJ} \sqrt{(\eta_y u^\xi + \xi_y u^\eta)^2 + (-\eta_x u^\xi - \xi_x u^\eta)^2} \end{aligned}$$

$$\begin{aligned} & \frac{\partial u^\eta}{\partial \tau} + (\xi_t + u^\xi) \frac{\partial u^\eta}{\partial \xi} + (\eta_t + u^\eta) \frac{\partial u^\eta}{\partial \eta} + \alpha_4 u^\xi u^\xi + \alpha_5 u^\xi u^\eta + \alpha_6 u^\eta u^\eta - D_\eta \\ &= -g \left[(\eta_x^2 + \eta_y^2) \frac{\partial H}{\partial \eta} (\xi_x \eta_x + \xi_y \eta_y) \frac{\partial H}{\partial \xi} \right] - \frac{C_f u^\eta}{hJ} \sqrt{(\eta_y u^\xi + \xi_y u^\eta)^2 + (-\eta_x u^\xi - \xi_x u^\eta)^2} \end{aligned}$$

Sediment transport eq.

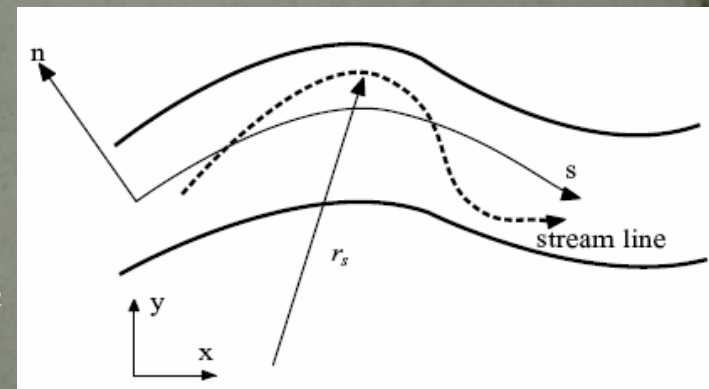
$$\frac{\partial z_b}{\partial t} + \frac{1}{1-\lambda} \left[\frac{\partial q_{bx}}{\partial x} + \frac{\partial q_{by}}{\partial y} \right] = 0$$

$$\frac{\partial}{\partial \tau} \left(\frac{z_b}{J} \right) + \frac{1}{1-\lambda} \left[\frac{\partial}{\partial \xi} \left(\frac{q^\xi}{J} \right) + \frac{\partial}{\partial \eta} \left(\frac{q^\eta}{J} \right) \right] = 0$$

where q^ξ, q^η = sediment transport rate components in the ξ, η direction, respectively.

$$q^\xi = \left(\xi_x \frac{\partial x}{\partial s} + \xi_y \frac{\partial y}{\partial s} \right) q^s + \left(\xi_x \frac{\partial x}{\partial n} + \xi_y \frac{\partial y}{\partial n} \right) q^n$$

$$q^\eta = \left(\eta_x \frac{\partial x}{\partial s} + \eta_y \frac{\partial y}{\partial s} \right) q^s + \left(\eta_x \frac{\partial x}{\partial n} + \eta_y \frac{\partial y}{\partial n} \right) q^n$$



Bank deformation

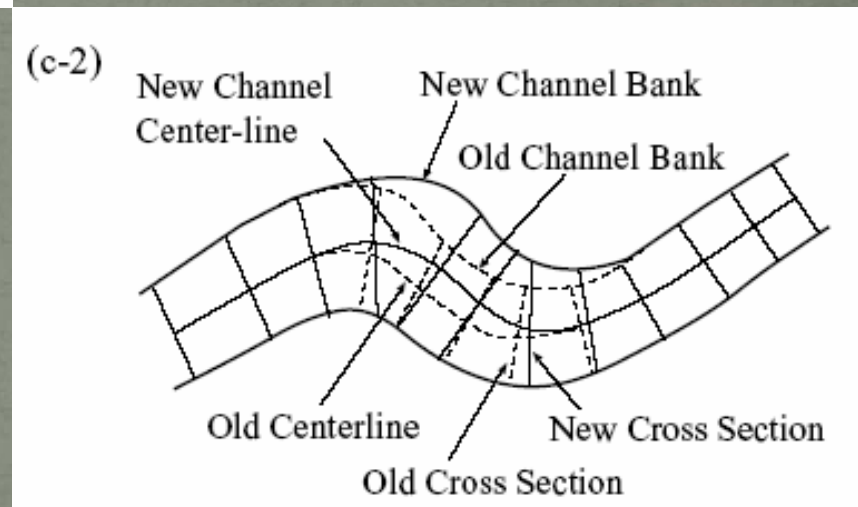
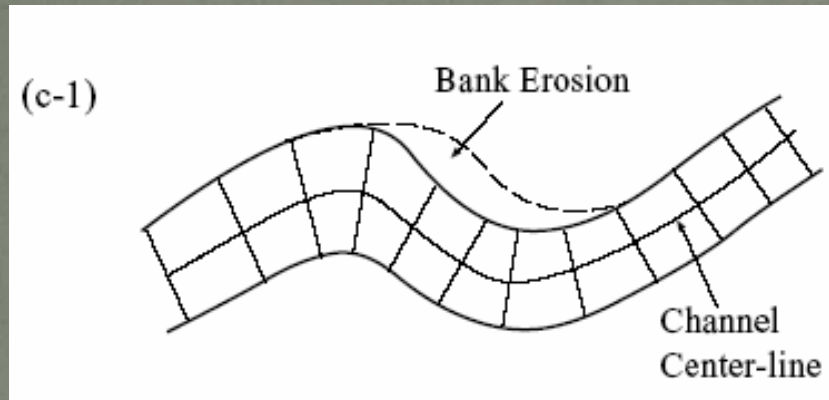


Fig. (c) bank deformation and renewal of the computational grid.

3. CIP Method

Alatna River, Alaska

(<http://www.ferragallria.com>)

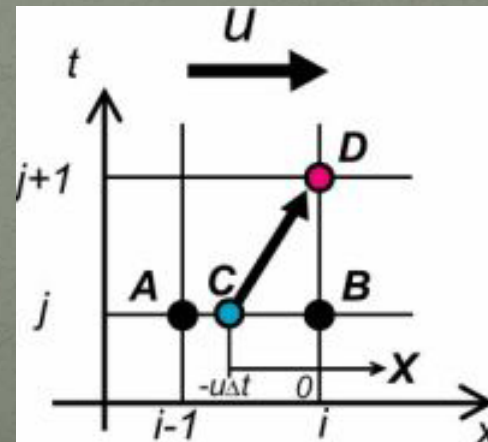
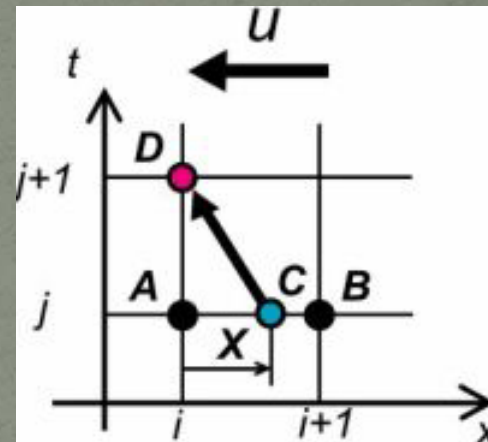
CIP method (Yabe et al., 1990)

C=Cubic, I=Interpolated, P=Pseudoparticle

$$\frac{\partial h}{\partial t} + u \frac{\partial f}{\partial x} = G$$

Advection phase: $\frac{\partial h}{\partial t} + u \frac{\partial f}{\partial x} = 0$

Diffusion phase: $\frac{\partial h}{\partial t} = G$



4. Calibration & Application

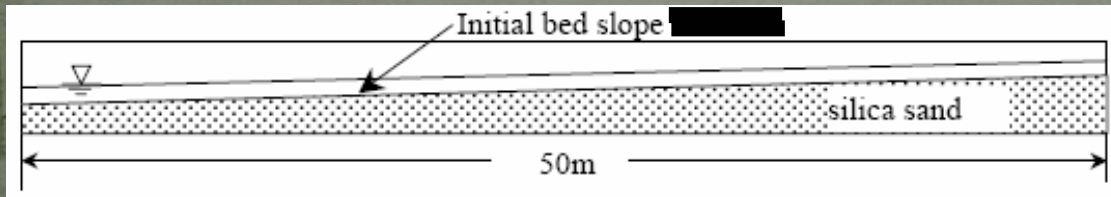
Alatna River, Alaska

(<http://www.ferragallria.com>)

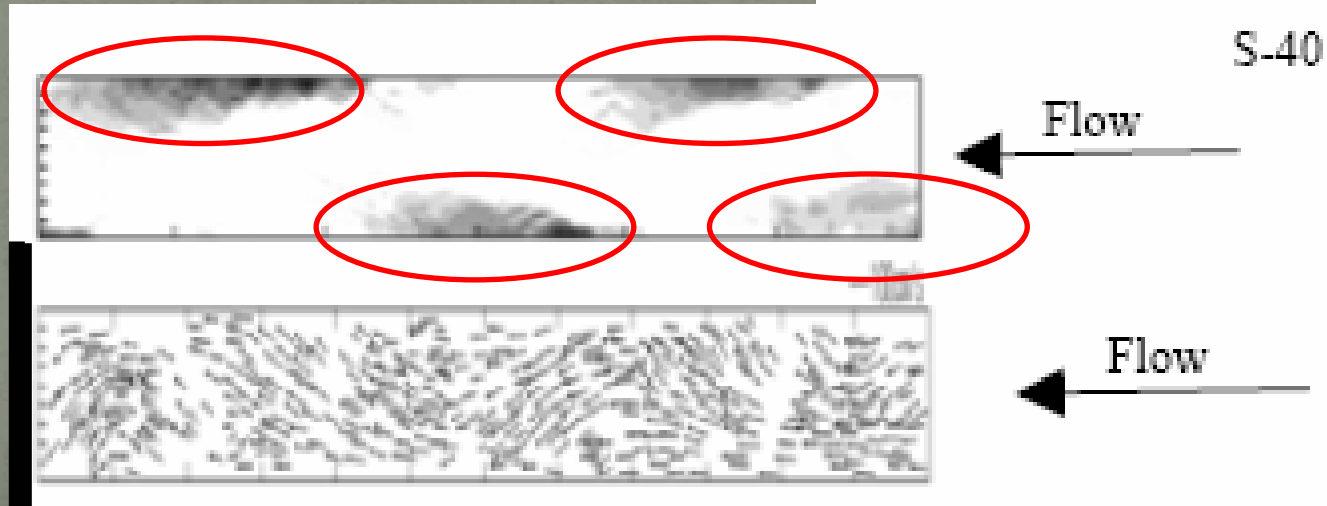
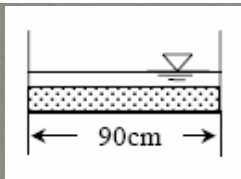
Watanabe et al., 2004

Run S-40

$L = 50.0$ m, $b = 0.90$ m, $q = 0.76$ l/s, $i_0 = 1/83$, $d = 0.75$ mm



Experiment



web number

$$\lambda = 0.45$$

non-dimensional height

$$Z_b = 2.80$$

Boundary Condition Test (S-40 no bank erosion)

Periodic boundary

non-Periodic condition

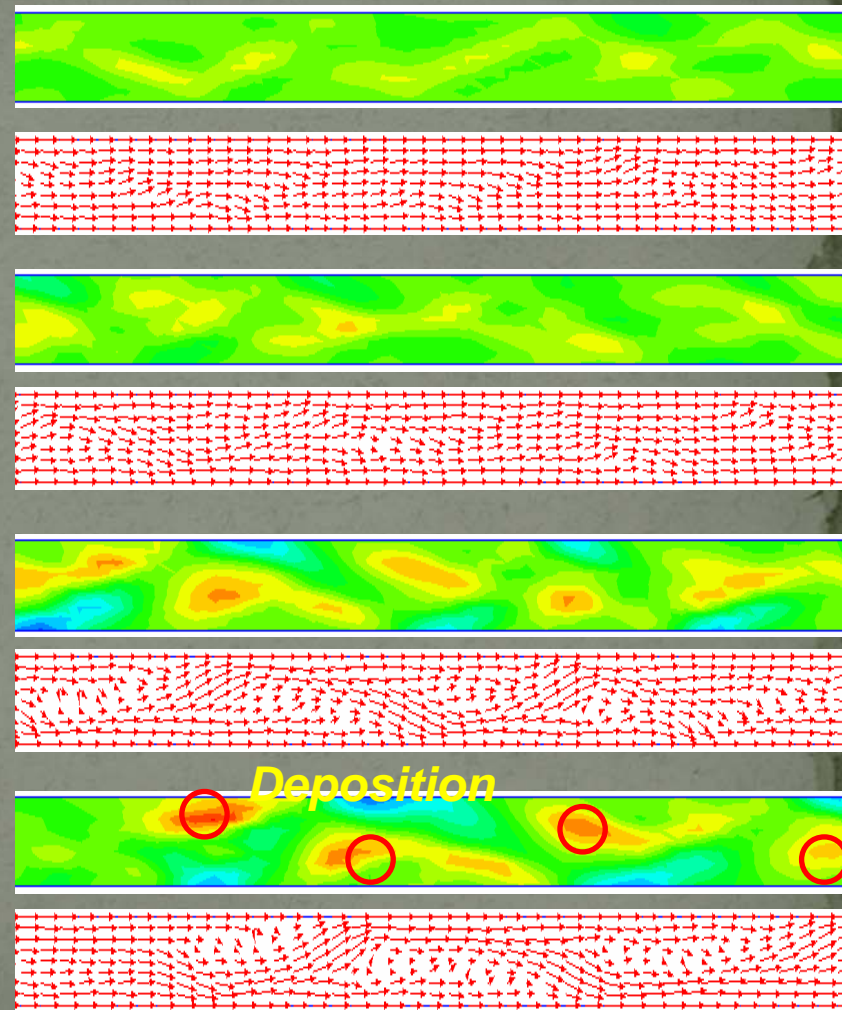
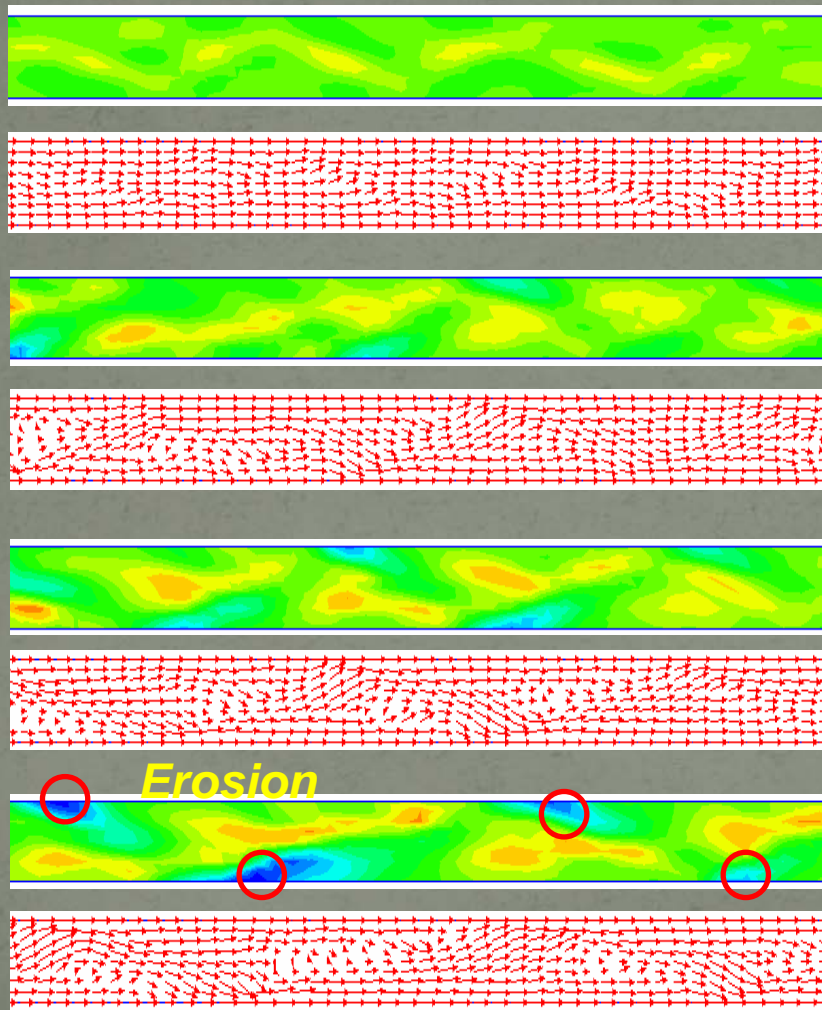
T(hr)

0.5

1.0

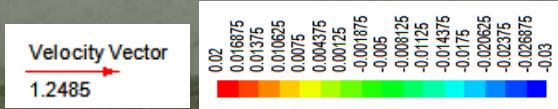
1.5

2.0



Erosion

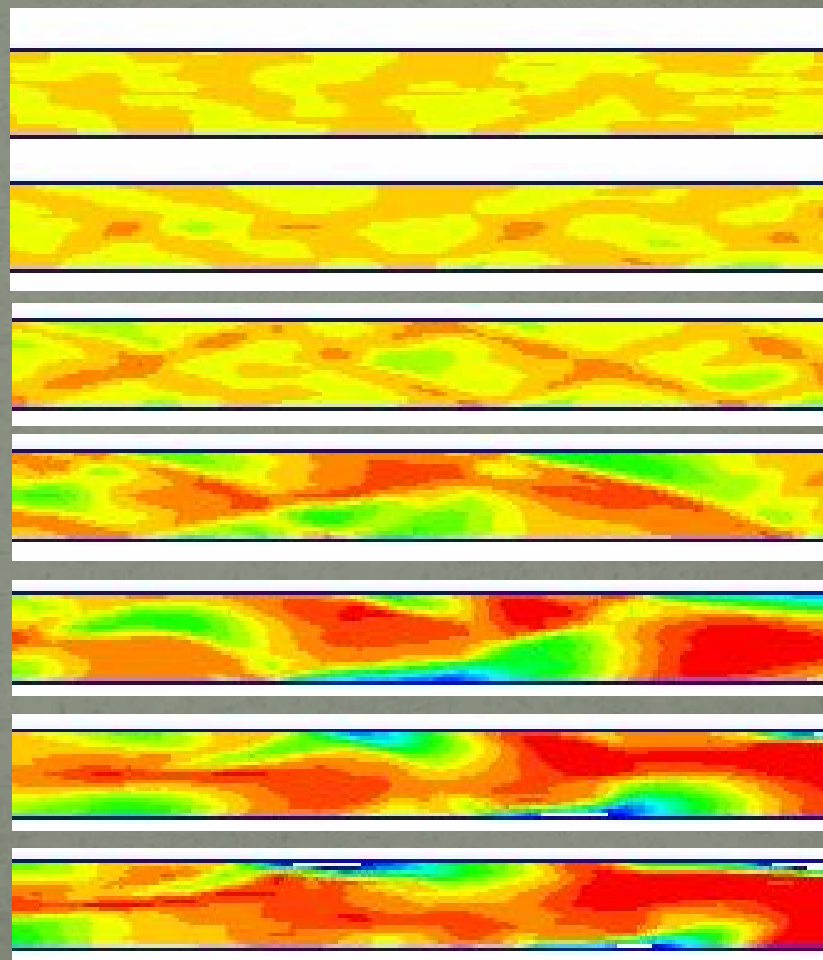
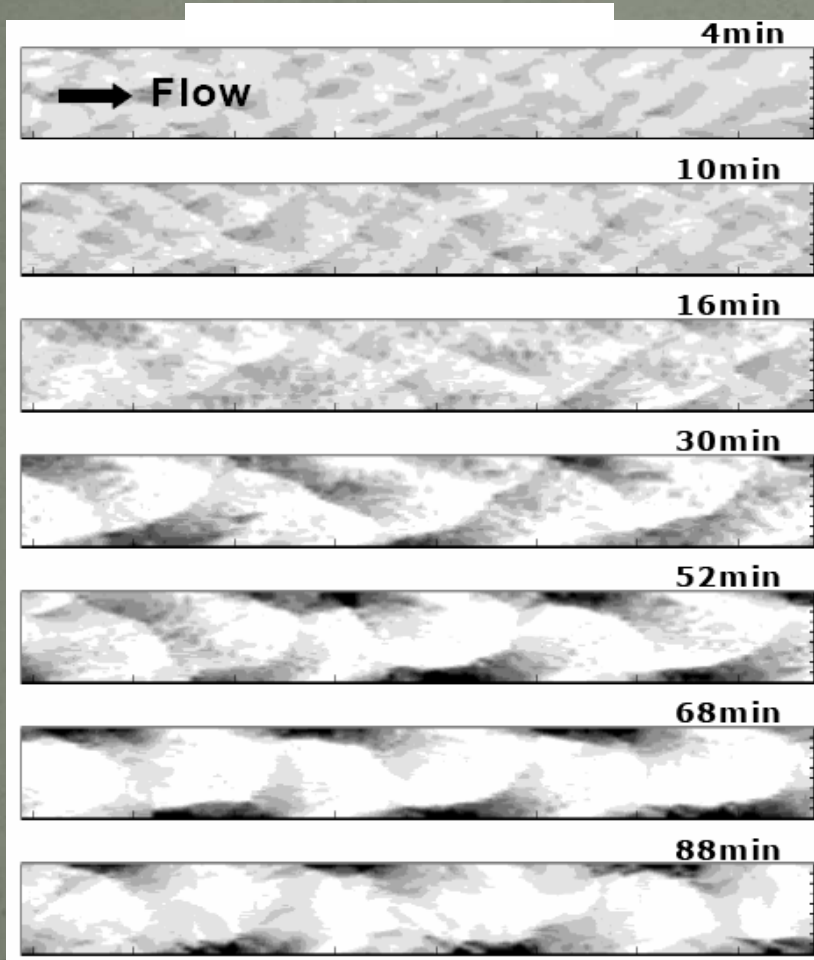
Deposition



Straight Channel (U-50 no bank erosion)

Experiment

Calculated



Straight Channel (U-30 no bank erosion)

T(min)

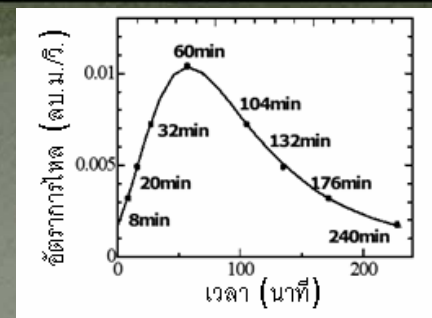
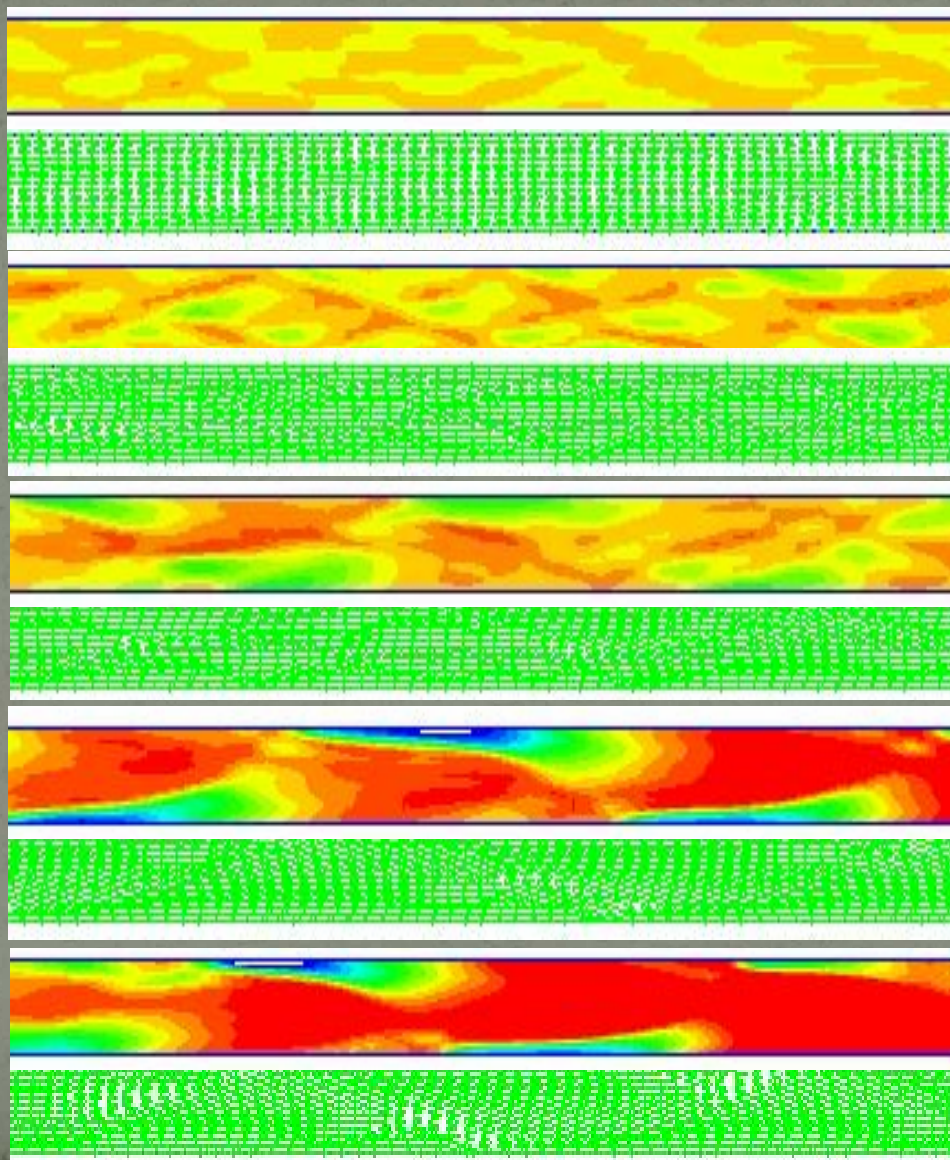
8

20

32

60

90



Straight Channel (U-30 with bank erosion)

T(min)

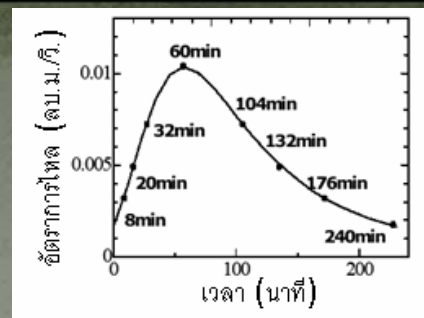
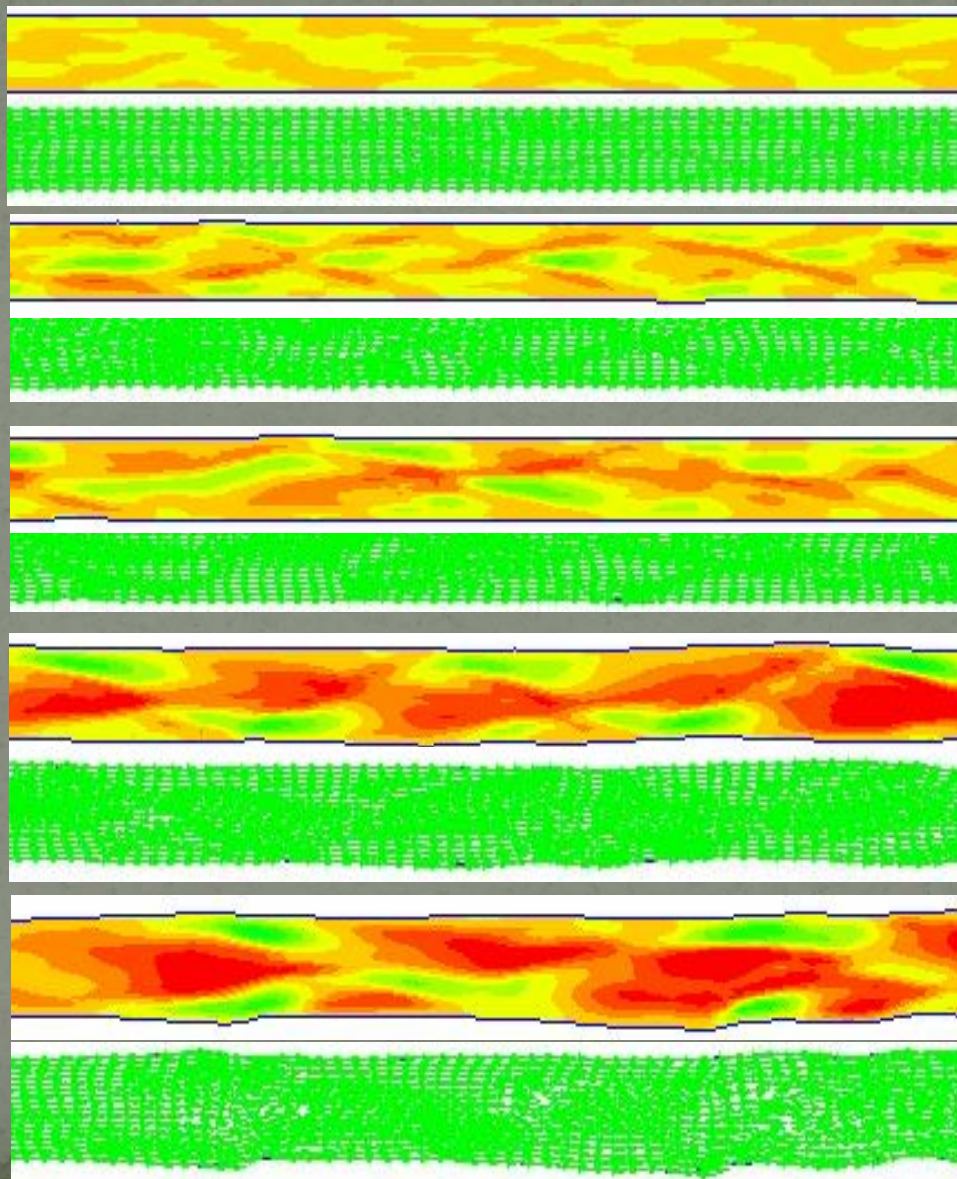
8

20

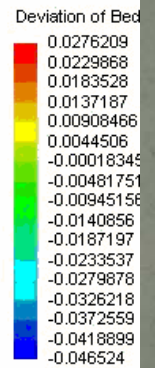
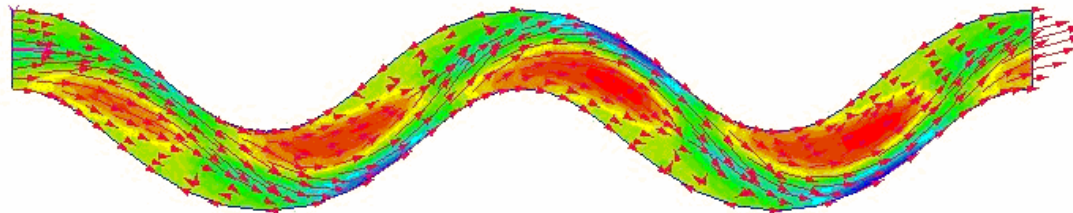
32

60

90



Sine-generated



Velocity Vector
1.20124

time [35] 175.000008 sec

Y
X

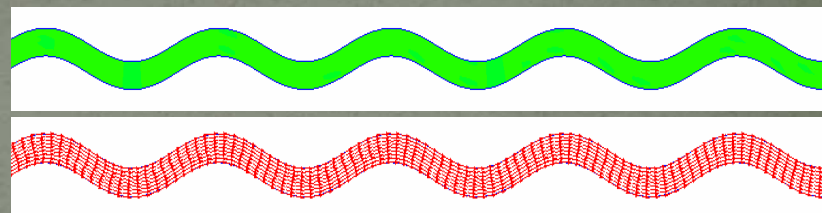
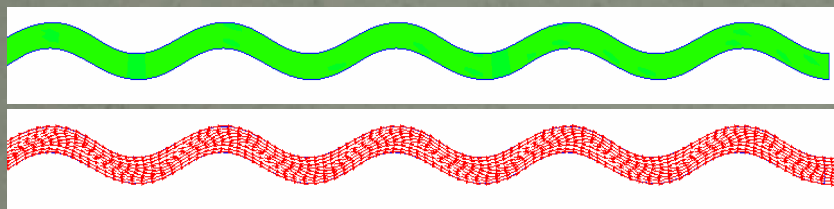
Sine-generated & Bank Erosion

Steady flow

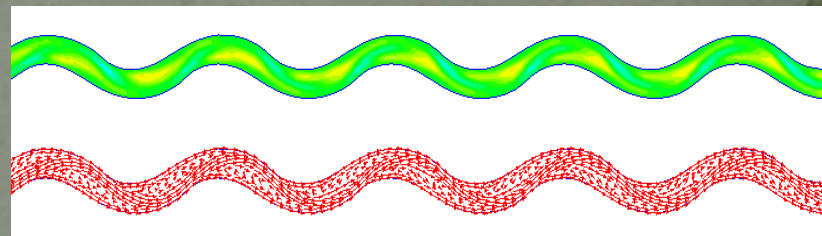
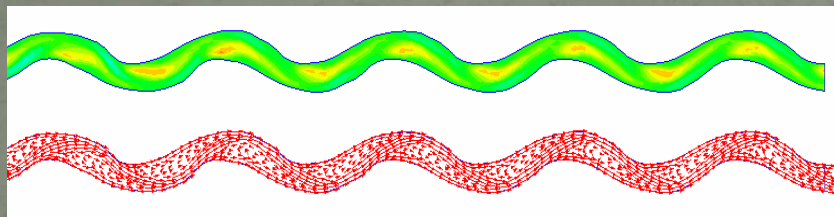
Unsteady flow

T(hr)

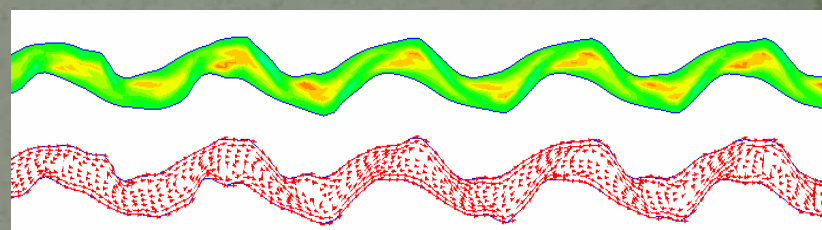
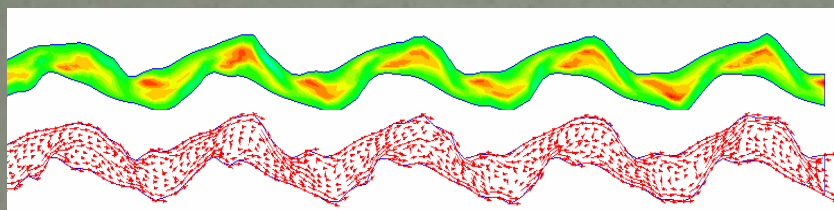
0.5



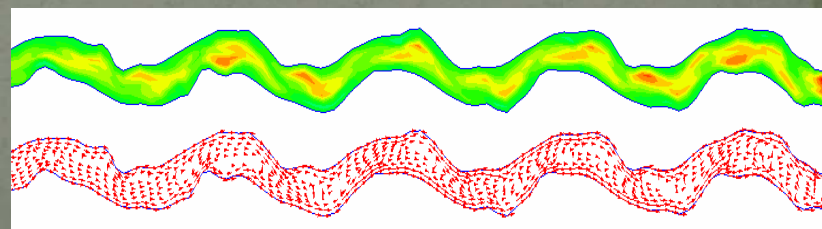
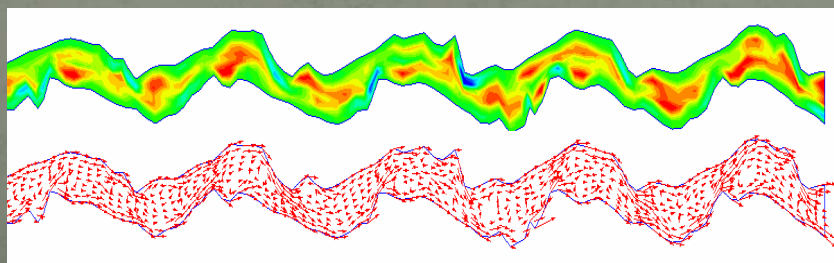
1.0



1.5



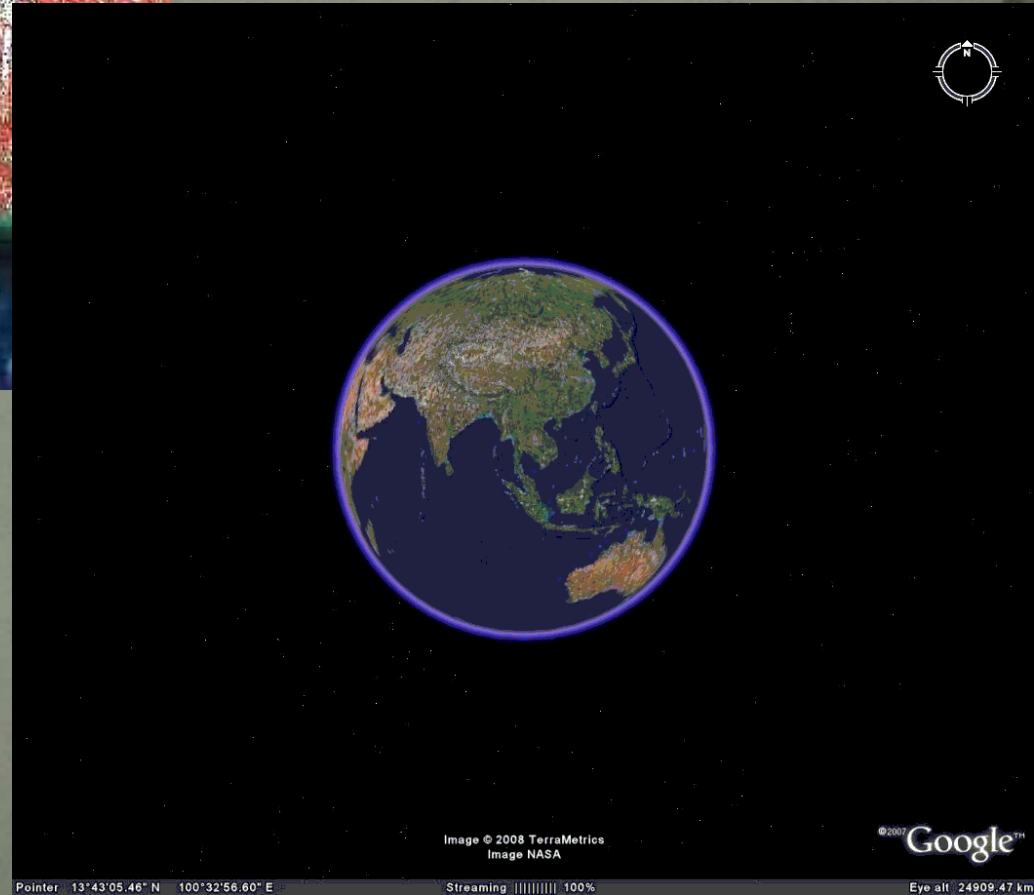
2.0



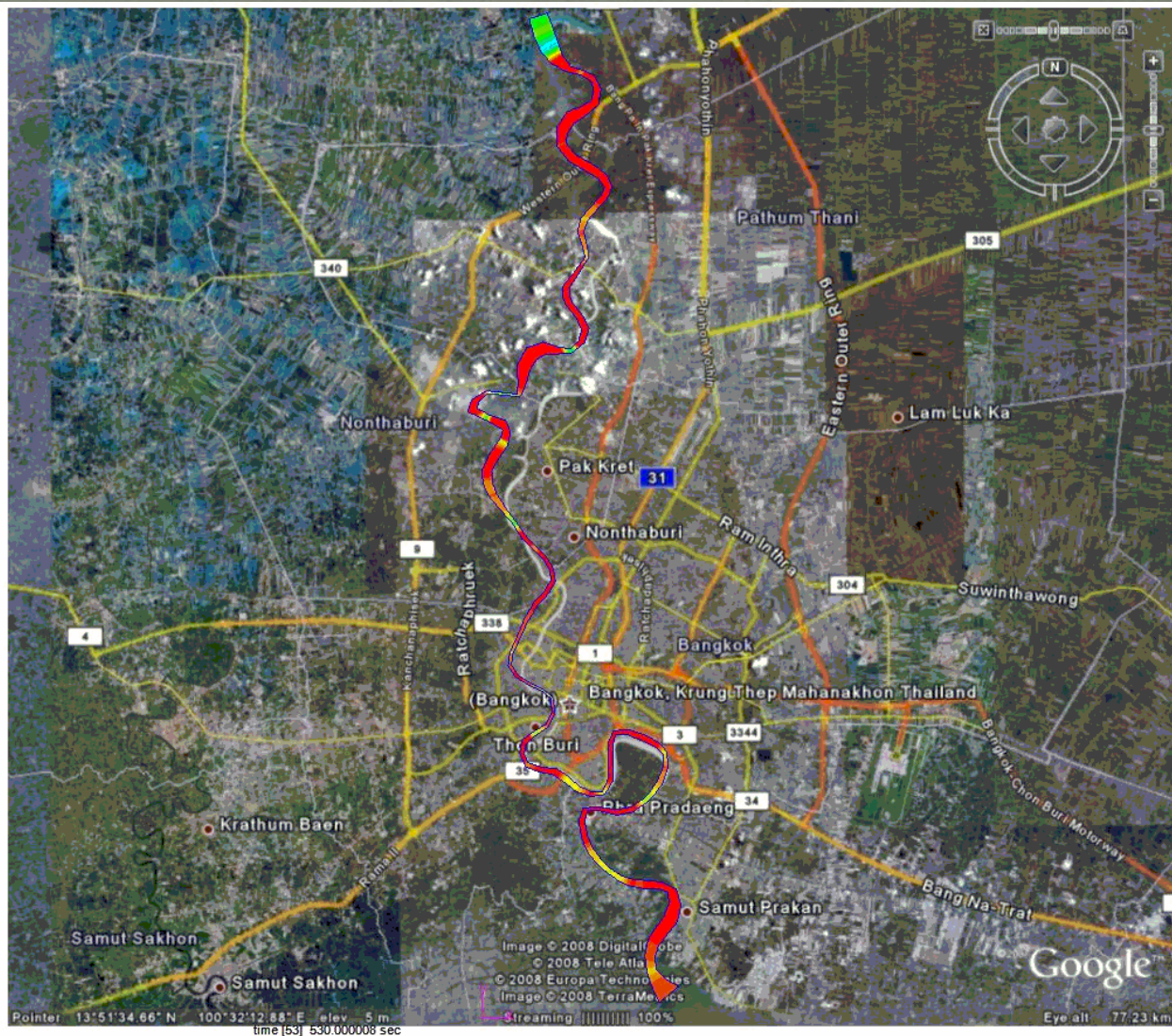
ChaoPhraya River



at Estuary

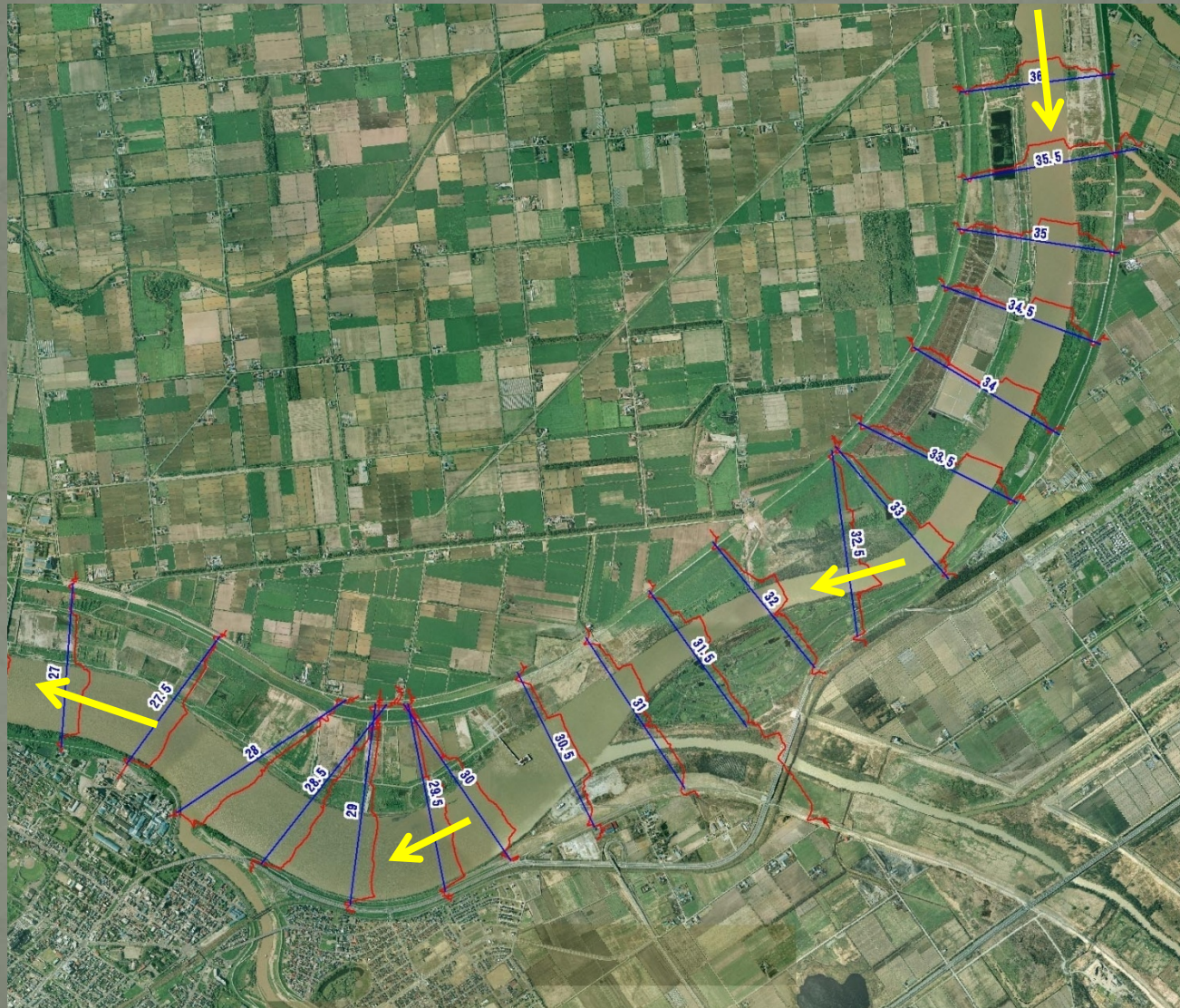


ChaoPhraya River



Y
Lx

Ishikari River



5. Conclusion

Alatna River, Alaska

(<http://www.ferragallery.com>)

Conclusions

- **2-D numerical model is proposed to investigate sand bed evolution in straight and meandering channel.**
- **CIP method has been proposed for solving water flow.**
- **Some numerical results compared with experiment data are presented to demonstrate applicability of the model.**
- **Good performances of simulated results were observed for channel evolutions under unsteady flow conditions, therefore, are indicating that the proposed model is reasonably achieved.**

THE END

