

# พฤติกรรมทางชลศาสตร์และแนวทางการออกแบบเขื่อนกันตลิ่ง

## HYDRAULICS BEHAVIOR AND DESIGN CONCEPTUAL OF SPUR DIKE



สนิท วงษา

มหาวิทยาลัยเทคโนโลยีพระจอมเกล้าธนบุรี

# Outlines

- Introduction
- Governing Equations
  - CIP Method
- Results
  - Design Conceptual



**Ushitsu River, Shikoku, Japan**

A large number of snow globes, each containing a different snowman design, displayed on a snowy surface. The snow globes are arranged in rows, and each one shows a unique snowman with various features like different colored sticks for noses, different colored buttons for mouths, and different colored sticks for arms. The snow globes are set against a background of snow.

# Introduction

Snow Festival, 2004



# Spur Dike



# Spur Dike







# Governing Equation

Snow Festival, 2004

**Continuity eq.**

$$\frac{\partial h}{\partial t} + \frac{\partial(hu)}{\partial x} + \frac{\partial(hv)}{\partial y} = 0$$

**Momentum eq.**

$$\frac{\partial(hu)}{\partial t} + \frac{\partial(hu^2)}{\partial x} + \frac{\partial(huv)}{\partial y} = -gh \frac{\partial H}{\partial x} - \frac{\tau_{bx}}{\rho} + \frac{\partial}{\partial x} \left[ \nu \frac{\partial(hu)}{\partial x} \right] + \frac{\partial}{\partial y} \left[ \nu \frac{\partial(hu)}{\partial y} \right]$$

$$\frac{\partial(hv)}{\partial t} + \frac{\partial(huv)}{\partial x} + \frac{\partial(hv^2)}{\partial y} = -gh \frac{\partial H}{\partial y} - \frac{\tau_{by}}{\rho} + \frac{\partial}{\partial x} \left[ \nu \frac{\partial(hv)}{\partial x} \right] + \frac{\partial}{\partial y} \left[ \nu \frac{\partial(hv)}{\partial y} \right]$$

where  $h$ = water depth,  $u, v$ = average velocity,  $\tau_b$ =shear stress,  $\rho$ =water density,  $H$ = water surface elevation ( $=z_b+h$ ),  $z_b$ =bed elevation,  $\nu$ = eddy viscosity,  $t$ =time, and  $x, y$ = spatial coordinate in Cartesian coordinate system.

## Cartesian coordinate system

### Bed shear stress

$$\tau_{bx} = \rho C_f u \sqrt{u^2 + v^2}$$

$$\tau_{by} = \rho C_f v \sqrt{u^2 + v^2}$$

### Eddy viscosity

$$\nu = \frac{\kappa}{6} u_* h$$

### Shear velocity

$$u_* = C_f \sqrt{u^2 + v^2}$$

where  $C_f$ =bed friction coefficient,  $\kappa$ =Karman's constant,  $u_*$ =shear velocity



**Bedload eq.****Kavacs&Parker eq.**

$$q_{bx} = \frac{17}{\cos \theta_b} \tau_*^{3/2} \left( 1 - \frac{\tau_{*c}}{\tau_*} \right) \left[ 1 - \sqrt{\frac{2\tau_{*c} \cos \theta_b}{\tau_*}} \right] + 2 \left( \tan \theta_b - \frac{\partial z_b}{\partial s} \right) \sqrt{sgd^3}$$

**Hasegawa eq.**

$$\frac{q_{by}}{\sqrt{sgd^3}} = q_{bx} \left( \frac{v}{u} - N_* \frac{h}{r_*} - \sqrt{\frac{\tau_{*c}}{v_s v_k \tau_*}} \frac{\partial z_b}{\partial y} \right)$$

where  $\tau_*$ =non-dimensional shear stress,  $\tau_c$ =critical shear stress,  $\tau_{*c}$ =critical non-dimension shear stress,  $\theta_b$ =bed slope,  $\rho_s$ =sediment density,  $s=(\rho_s/\rho-1)$ ,  $N_*$ =Engelund's constant, and  $r_*$ =radius of curvature.

$$\frac{1}{r_*} = \frac{1}{(u^2 + v^2)^{3/2}} \left\{ u \left( u \frac{\partial v}{\partial x} - v \frac{\partial u}{\partial x} \right) + v \left( u \frac{\partial v}{\partial y} - v \frac{\partial u}{\partial y} \right) \right\}$$

**Sediment transport eq.**

$$\frac{\partial z_b}{\partial t} + \frac{1}{1-\lambda} \left[ \frac{\partial q_{bx}}{\partial x} + \frac{\partial q_{by}}{\partial y} \right] = 0$$

where  $z_b$ =bed elevation,  $\lambda$ =porosity of bed material.

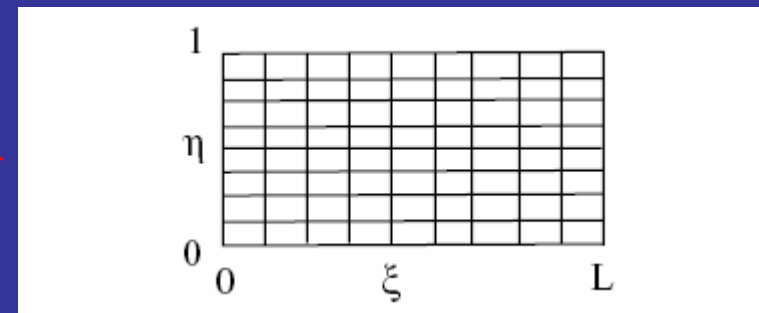
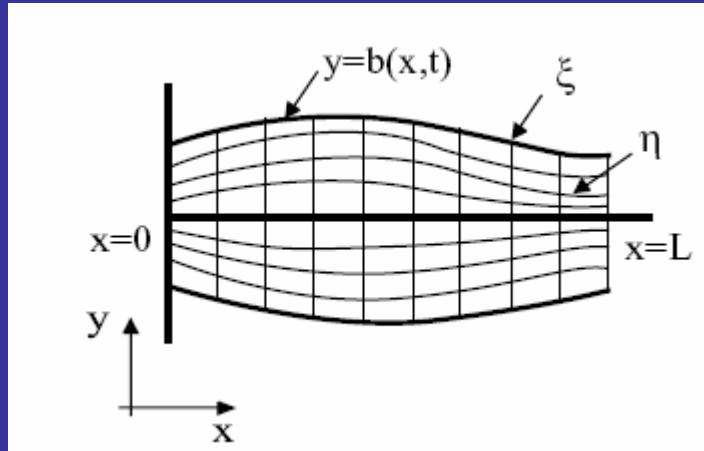


# Transformed rule

$$\begin{pmatrix} \frac{\partial}{\partial t} \\ \frac{\partial}{\partial x} \\ \frac{\partial}{\partial y} \end{pmatrix} = \begin{pmatrix} \tau_t & \xi_t & \eta_t \\ \tau_x & \xi_x & \eta_x \\ \tau_y & \xi_y & \eta_y \end{pmatrix} \begin{pmatrix} \frac{\partial}{\partial \tau} \\ \frac{\partial}{\partial \xi} \\ \frac{\partial}{\partial \eta} \end{pmatrix}$$

$$\begin{pmatrix} u \\ v \end{pmatrix} = \frac{1}{J} \begin{pmatrix} \eta_y & -\xi_y \\ -\eta_x & \xi_x \end{pmatrix} \begin{pmatrix} u^\xi \\ v^\eta \end{pmatrix}$$

where  $u^\xi, v^\eta$  = average velocity components in the of  $\xi, \eta$  direction,  $\tau$  = time, and  $J$  = Jacobian of coordinate transformed.





# Moving boundary-fitted system

## Continuity eq.

$$\frac{\partial}{\partial \tau} \left( \frac{h}{J} \right) + \frac{\partial}{\partial \xi} \left[ (\xi_t + u^\xi) \frac{h}{J} \right] + \frac{\partial}{\partial \eta} \left[ (\eta_t + u^\eta) \frac{h}{J} \right] = 0$$

## Momentum eq.

$$\begin{aligned} & \frac{\partial u^\xi}{\partial \tau} + (\xi_t + u^\xi) \frac{\partial u^\xi}{\partial \xi} + (\eta_t + u^\eta) \frac{\partial u^\xi}{\partial \eta} + \alpha_1 u^\xi u^\xi + \alpha_2 u^\xi u^\eta + \alpha_3 u^\eta u^\eta - D_\xi \\ &= -g \left[ (\xi_x^2 + \xi_y^2) \frac{\partial H}{\partial \xi} (\xi_x \eta_x + \xi_y \eta_y) \frac{\partial H}{\partial \eta} \right] - \frac{C_f u^\xi}{hJ} \sqrt{(\eta_y u^\xi + \xi_y u^\eta)^2 + (-\eta_x u^\xi - \xi_x u^\eta)^2} \end{aligned}$$

$$\begin{aligned} & \frac{\partial u^\eta}{\partial \tau} + (\xi_t + u^\xi) \frac{\partial u^\eta}{\partial \xi} + (\eta_t + u^\eta) \frac{\partial u^\eta}{\partial \eta} + \alpha_4 u^\xi u^\xi + \alpha_5 u^\xi u^\eta + \alpha_6 u^\eta u^\eta - D_\eta \\ &= -g \left[ (\eta_x^2 + \eta_y^2) \frac{\partial H}{\partial \eta} (\xi_x \eta_x + \xi_y \eta_y) \frac{\partial H}{\partial \xi} \right] - \frac{C_f u^\eta}{hJ} \sqrt{(\eta_y u^\xi + \xi_y u^\eta)^2 + (-\eta_x u^\xi - \xi_x u^\eta)^2} \end{aligned}$$

# Moving boundary-fitted system

## Sediment transport eq.

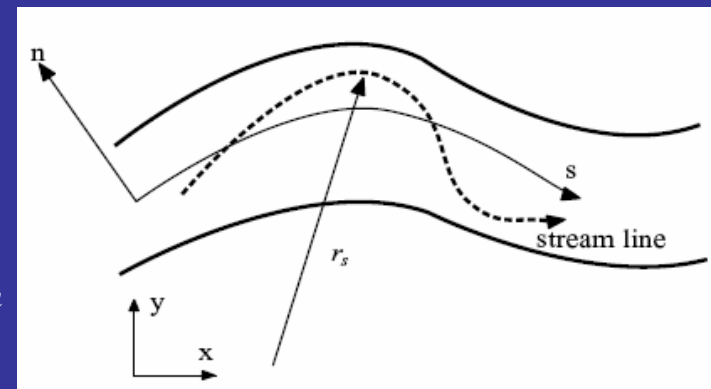
$$\frac{\partial z_b}{\partial t} + \frac{1}{1-\lambda} \left[ \frac{\partial q_{bx}}{\partial x} + \frac{\partial q_{by}}{\partial y} \right] = 0$$

$$\frac{\partial}{\partial \tau} \left( \frac{z_b}{J} \right) + \frac{1}{1-\lambda} \left[ \frac{\partial}{\partial \xi} \left( \frac{q^\xi}{J} \right) + \frac{\partial}{\partial \eta} \left( \frac{q^\eta}{J} \right) \right] = 0$$

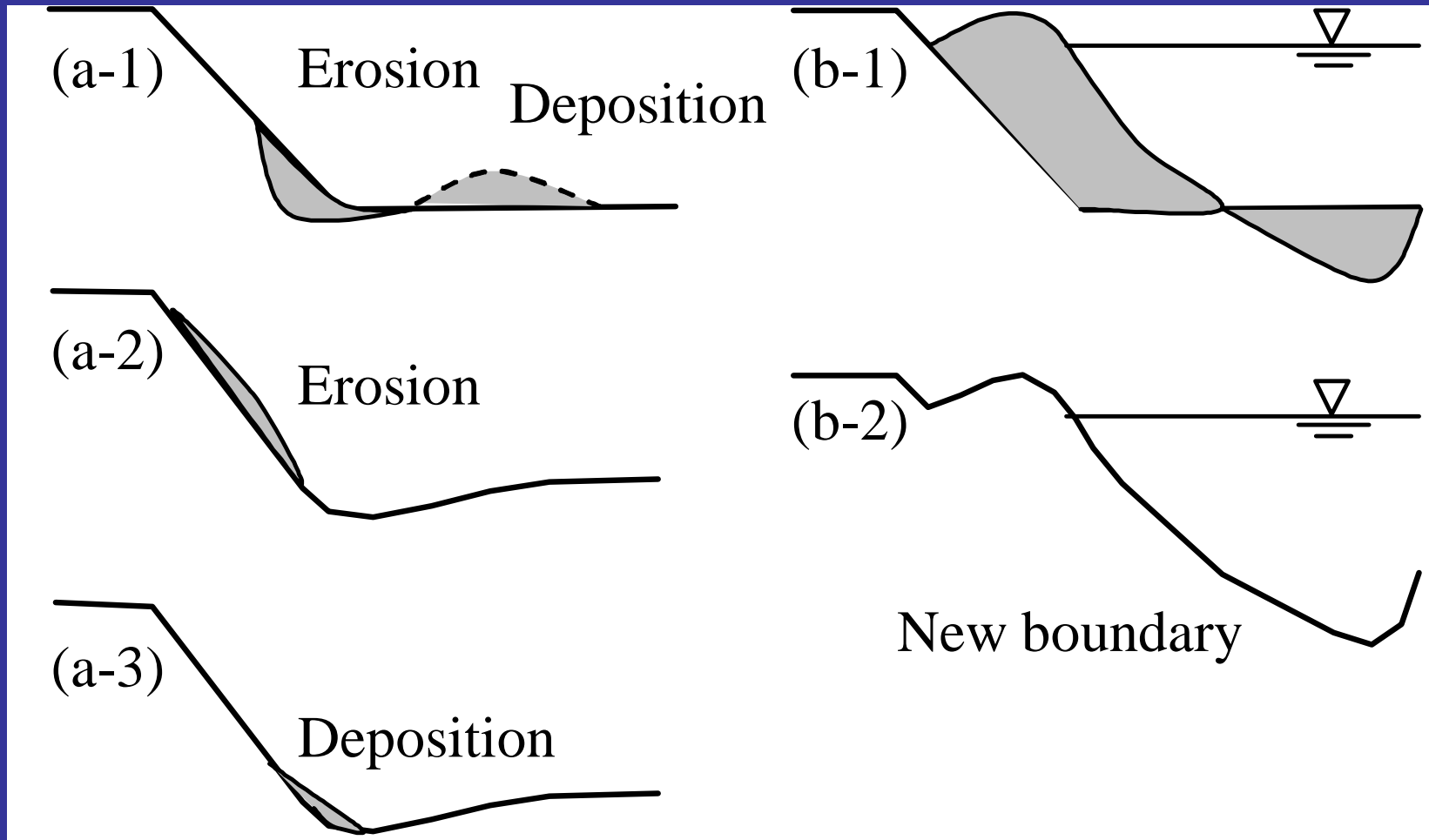
where  $q^\xi, q^\eta$  = sediment transport rate components in the  $\xi, \eta$  direction, respectively.

$$q^\xi = \left( \xi_x \frac{\partial x}{\partial s} + \xi_y \frac{\partial y}{\partial s} \right) q^s + \left( \xi_x \frac{\partial x}{\partial n} + \xi_y \frac{\partial y}{\partial n} \right) q^n$$

$$q^\eta = \left( \eta_x \frac{\partial x}{\partial s} + \eta_y \frac{\partial y}{\partial s} \right) q^s + \left( \eta_x \frac{\partial x}{\partial n} + \eta_y \frac{\partial y}{\partial n} \right) q^n$$



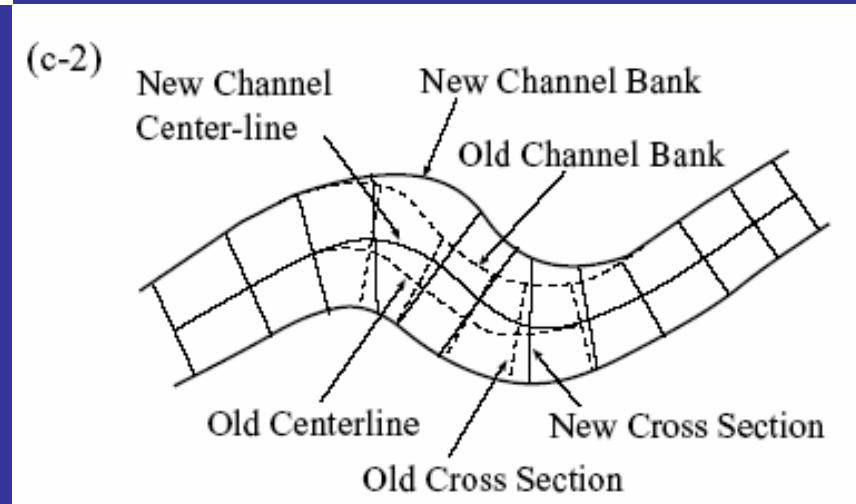
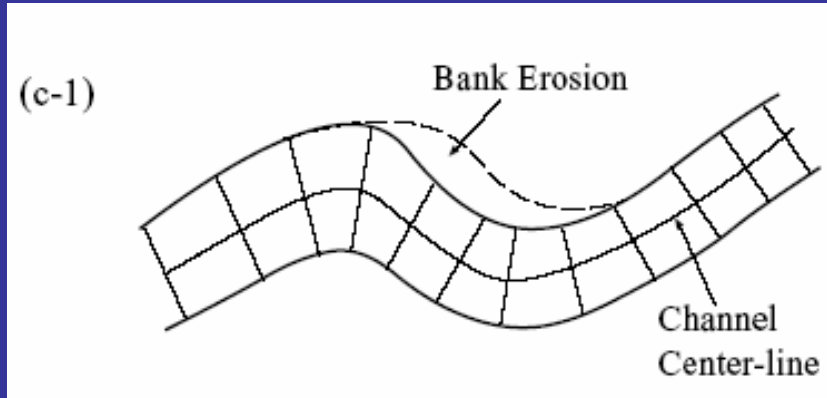
# Bank erosion mechanisms



**Fig. (a) bank erosion and migration, (b) bed aggradation and bank deposition.**



# Bank deformation



**Fig. (c) bank deformation and renewal of the computational grid.**



# CIP Method

Snow Festival, 2004

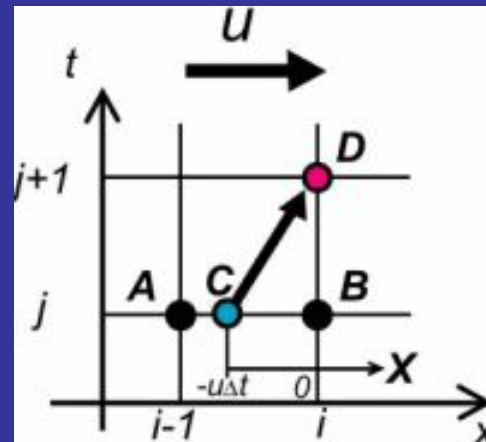
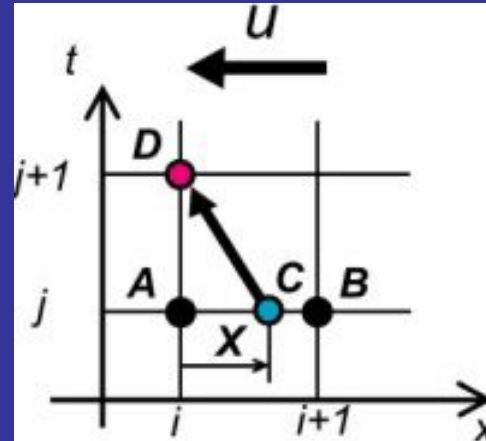
# CIP method (Yabe et al., 1990)

**C=Cubic, I=Interpolated, P=Psuedoparticle**


$$\frac{\partial h}{\partial t} + u \frac{\partial f}{\partial x} = G$$

Advection phase:  $\frac{\partial h}{\partial t} + u \frac{\partial f}{\partial x} = 0$

Diffusion phase:  $\frac{\partial h}{\partial t} = G$







# Results

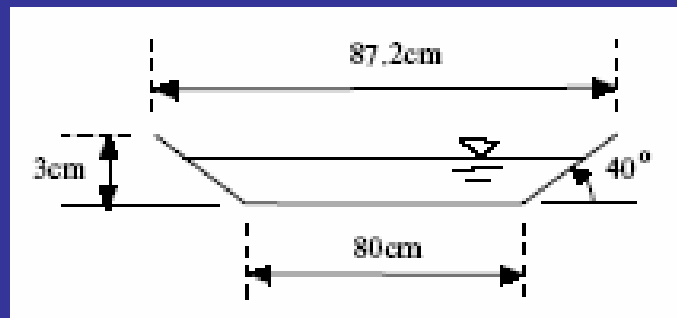
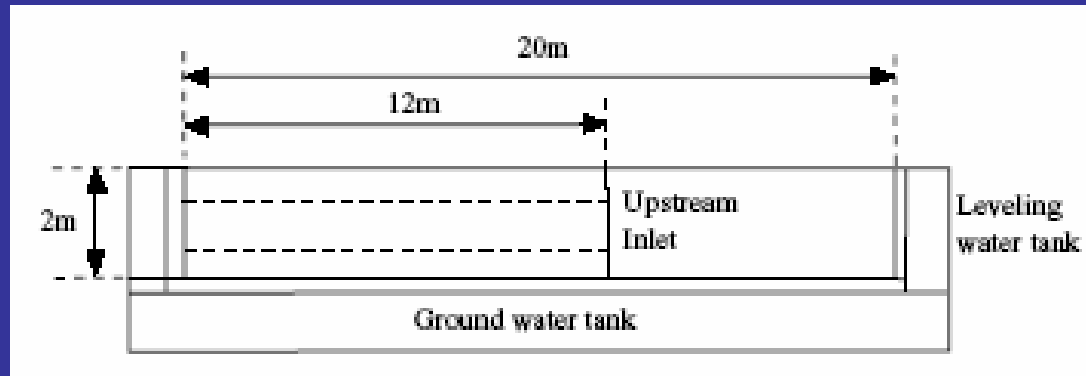
Snow Festival, 2004

# Jang & Shimizu, 2003

## Conditions

$L = 12.0 \text{ m}$ ,  $b = 0.80 \text{ m}$ ,  $q = 4.50 \text{ l/s}$ ,  $i = 1.0\%$ ,  $\theta = 40^\circ$

$d = 1.25 \text{ mm}$

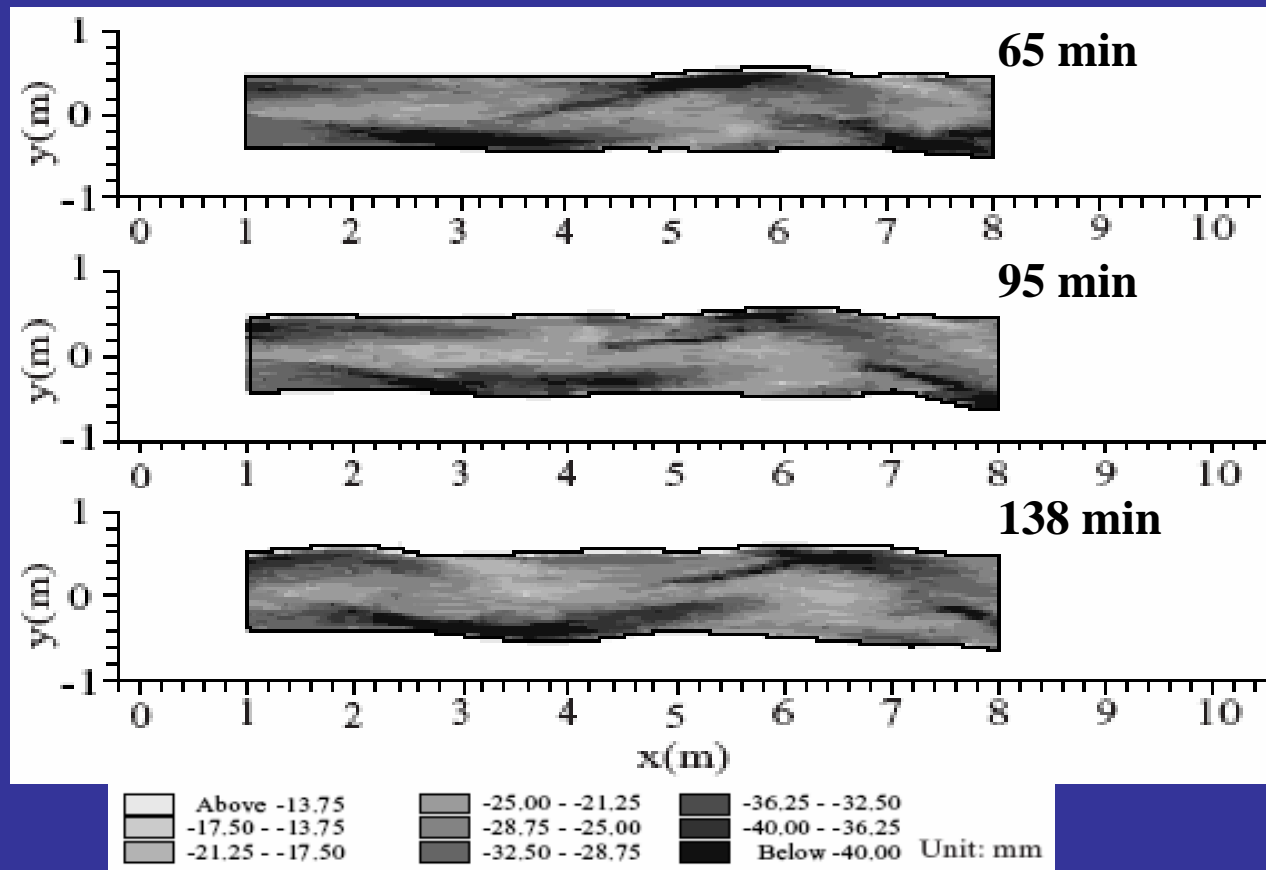


## Experiment



# Jang&Shimizu, 2003

## Experiment Results





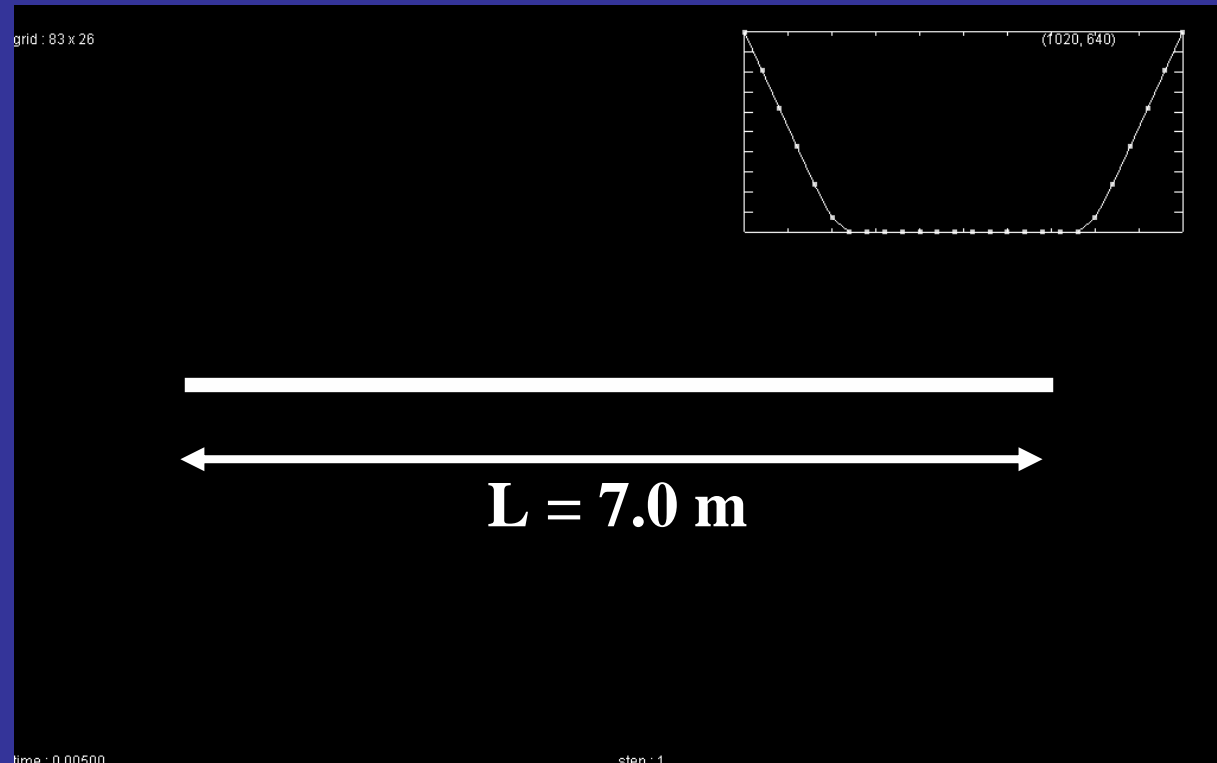
# Jang&Shimizu, 2003

## Conditions

$$L = 12.0 \text{ m}, b = 0.80 \text{ m}, q = 4.50 \text{ l/s}, i = 1.0\%$$

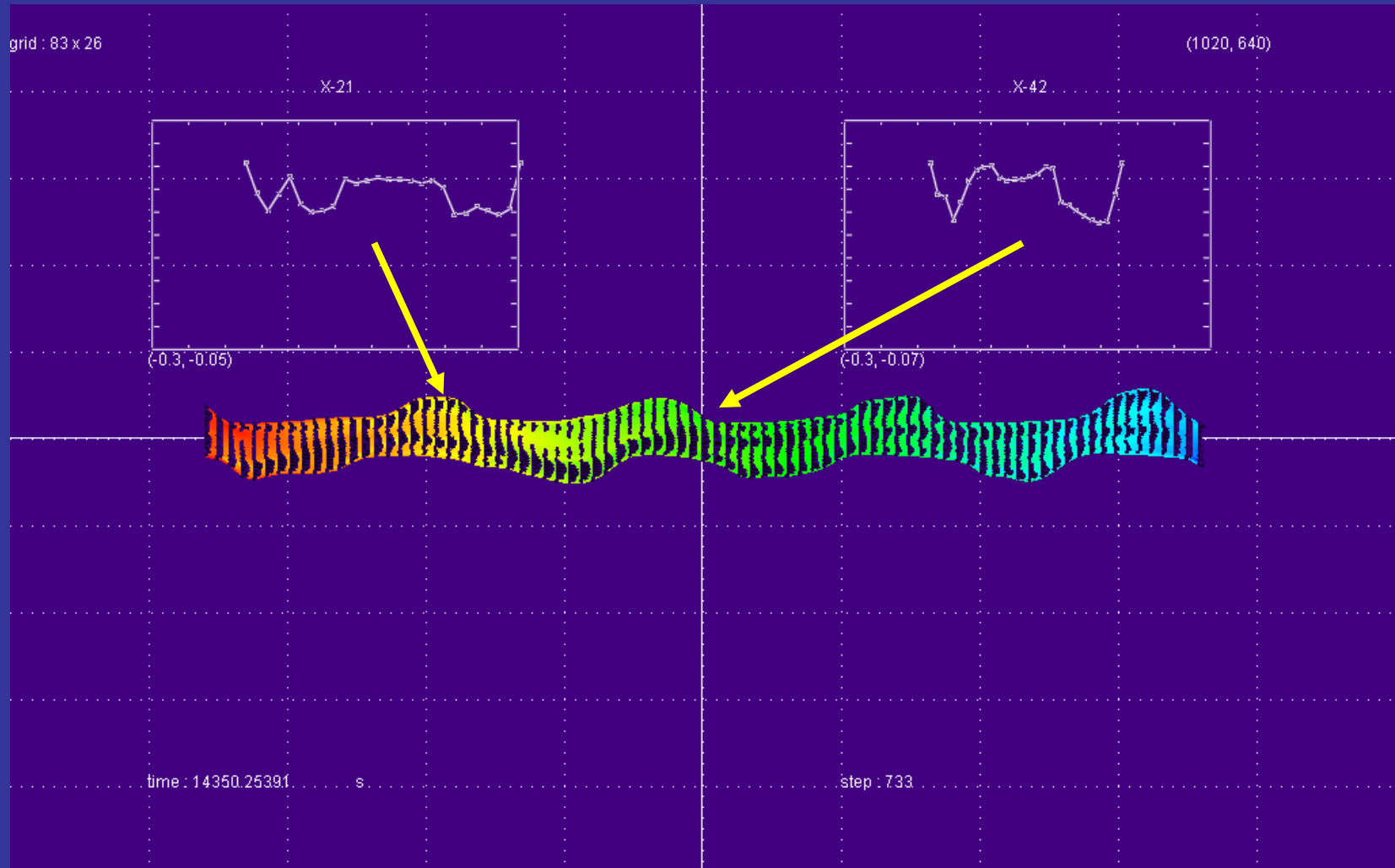
$$n_x = 83, n_y = 26, \Delta x = 0.1463 \text{ m}, \Delta y = 0.0038 \text{ m}, \Delta t = 0.005 \text{ s},$$

$$d = 1.25 \text{ mm}$$



Initial grid

# Flow vector and bank deformation

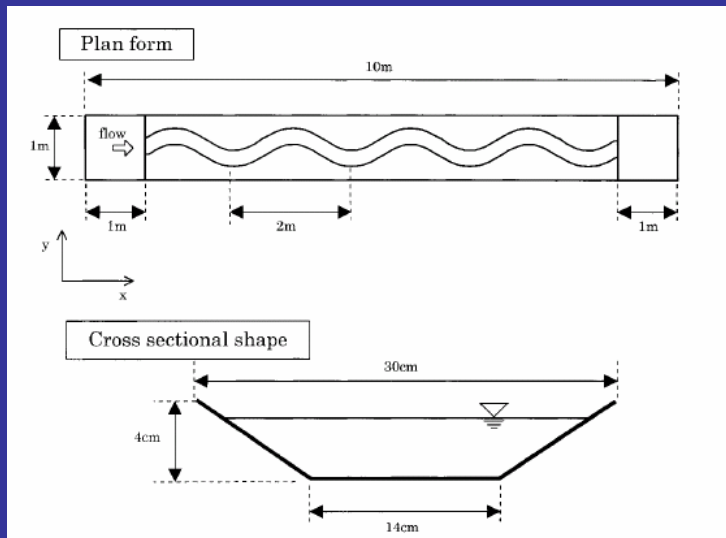


# Run3- Nagata et al., 2000

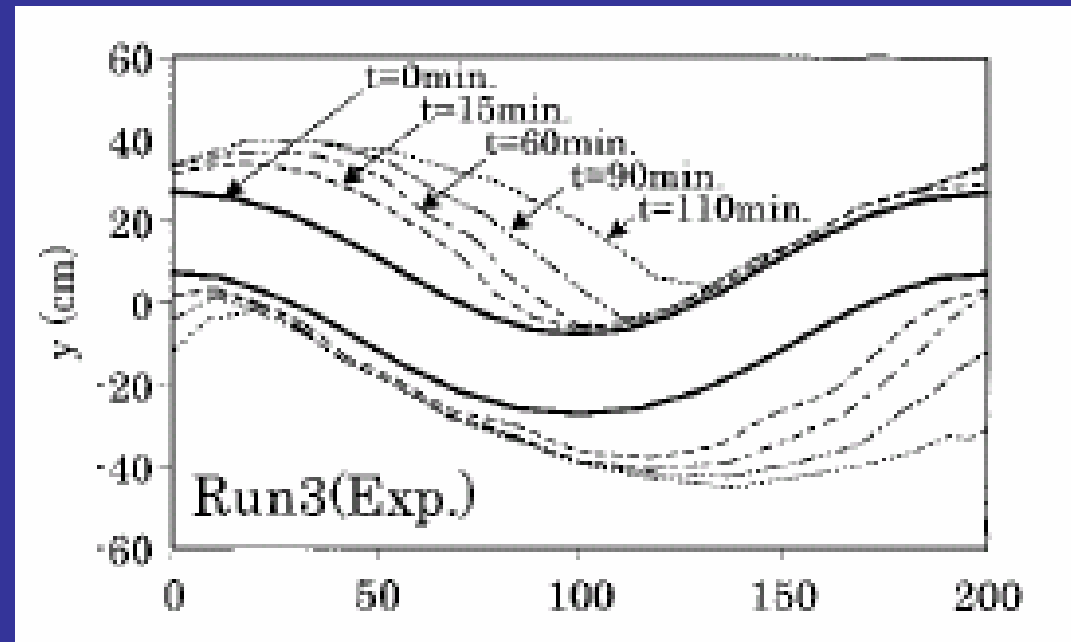
## Conditions

$L = 10.0$  m,  $B = 0.30$  m,  $q = 1.98$  l/s,  $i = 1.0\%$

$d = 1.42$  mm



## Experiment



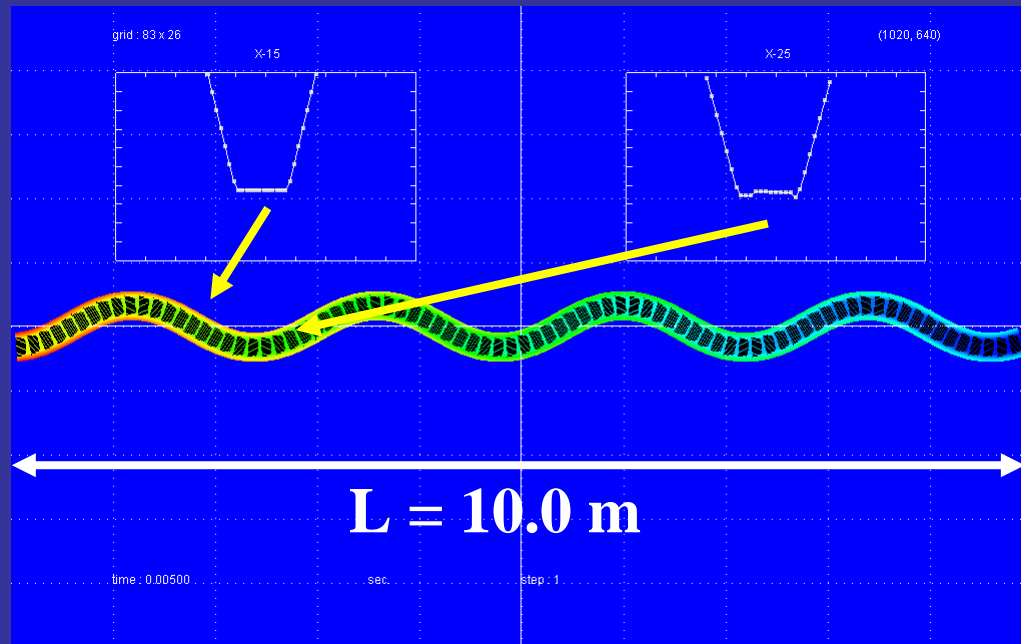
# Run3- Nagata et al., 2000

## Conditions

$L = 10.0$  m,  $B = 0.30$  m,  $q = 1.98$  l/s,  $i = 1.0\%$

$n_x = 83$ ,  $n_y = 26$ ,  $\Delta x = 0.128$  m,  $\Delta y = 0.0054$  m,  $\Delta t = 0.005$  s,

$d = 1.42$  mm



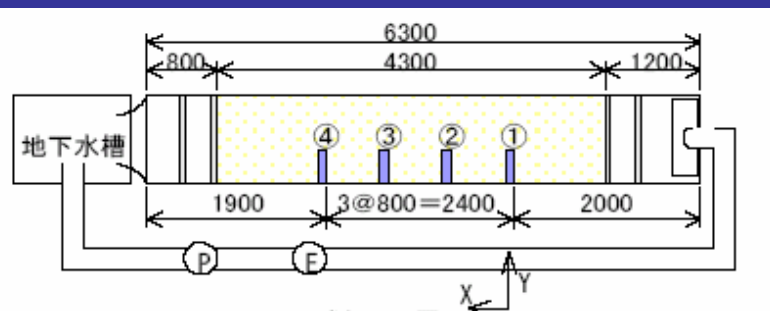
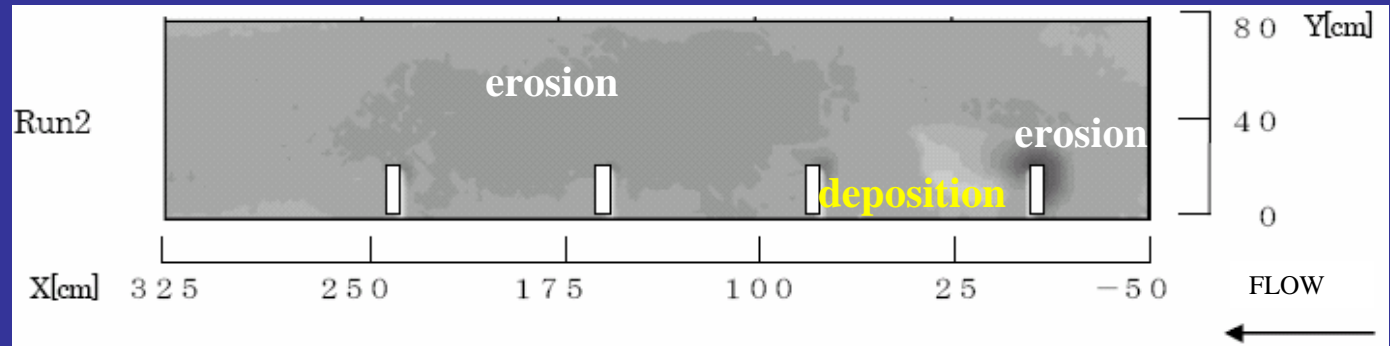
Initial grid

# Run2- Morita et al., 2005

## Conditions

$L = 6.30$  m,  $B = 0.80$  m,  $q = 8.25$  l/s,  $i = 1/2000$

$d = 0.88$  mm



## Experiment



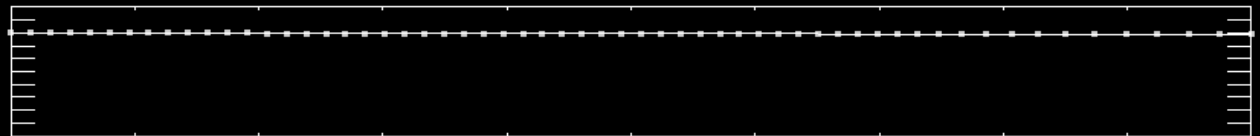
# Run2- Morita et al., 2005

## Conditions

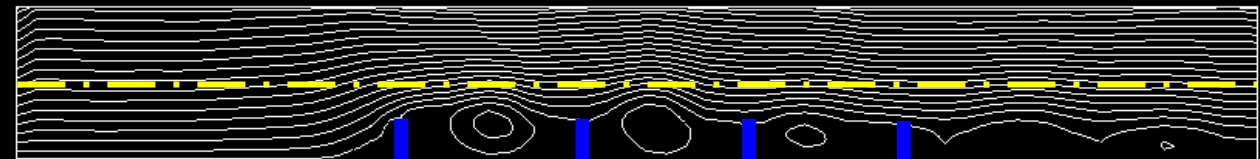
$L = 6.30$  m,  $B = 0.80$  m,  $q = 8.25$  l/s,  $i = 1/2000$

$n_x = 50$ ,  $n_y = 20$ ,  $\Delta x = 0.126$  m,  $\Delta y = 0.04$  m,  $\Delta t = 0.002$  s,

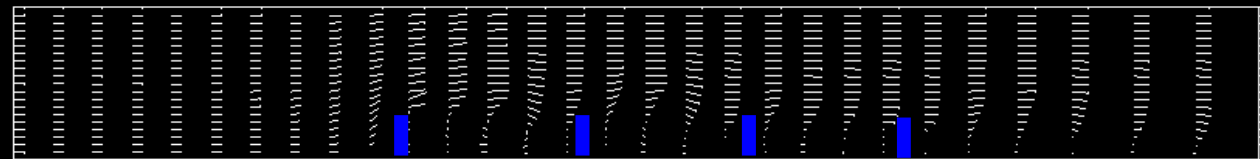
Bed elevation



Streamline



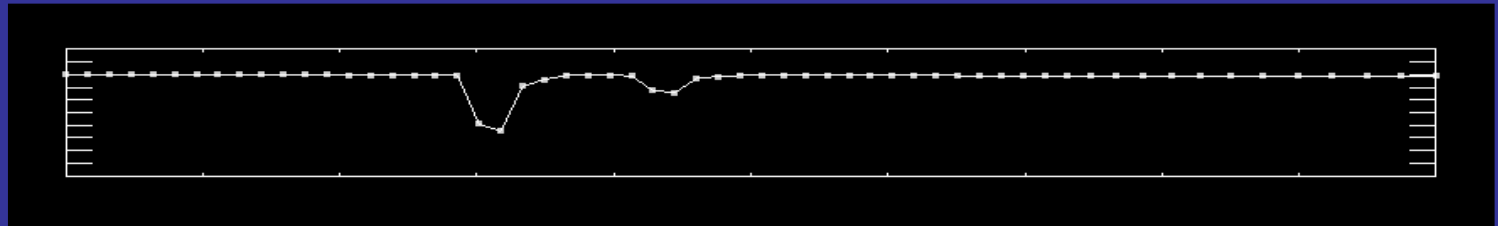
Velocity vector



Initial condition

# Run2- Morita et al., 2005

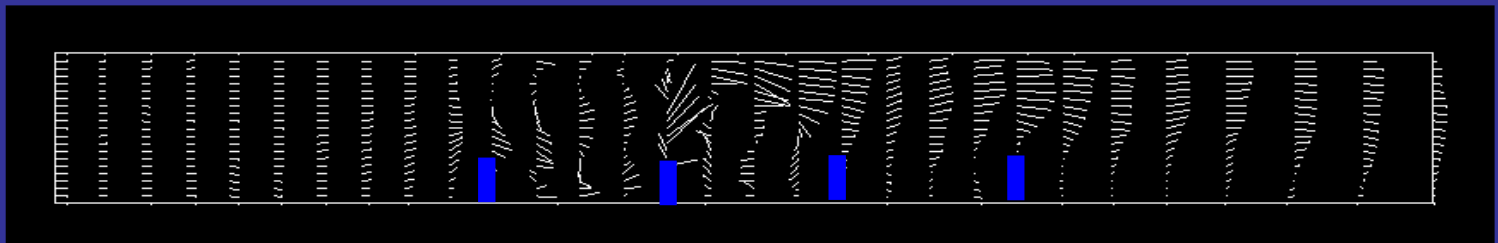
Bed elevation



Streamline



Velocity vector

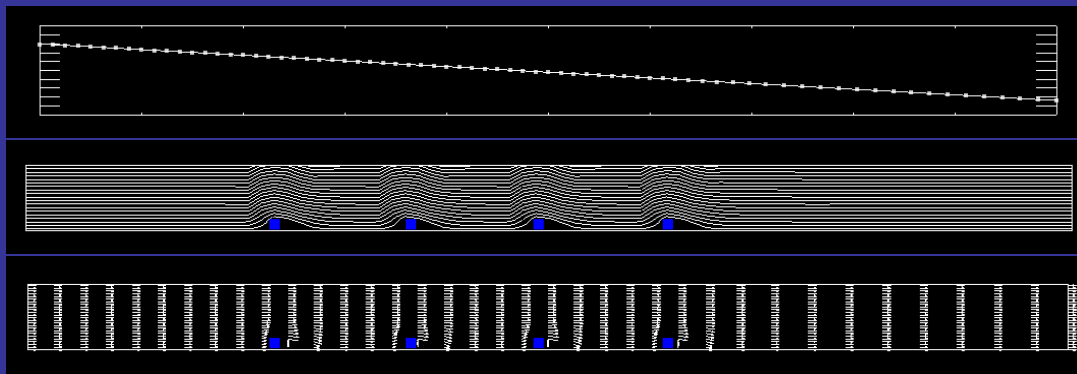


$t = 120$  min.

# Application 1

## Conditions

$L = 80.0$  m,  $B = 10.0$  m,  $q = 50$  m<sup>3</sup>/s,  $i = 1/2000$ ,  $d = 1.45$  mm



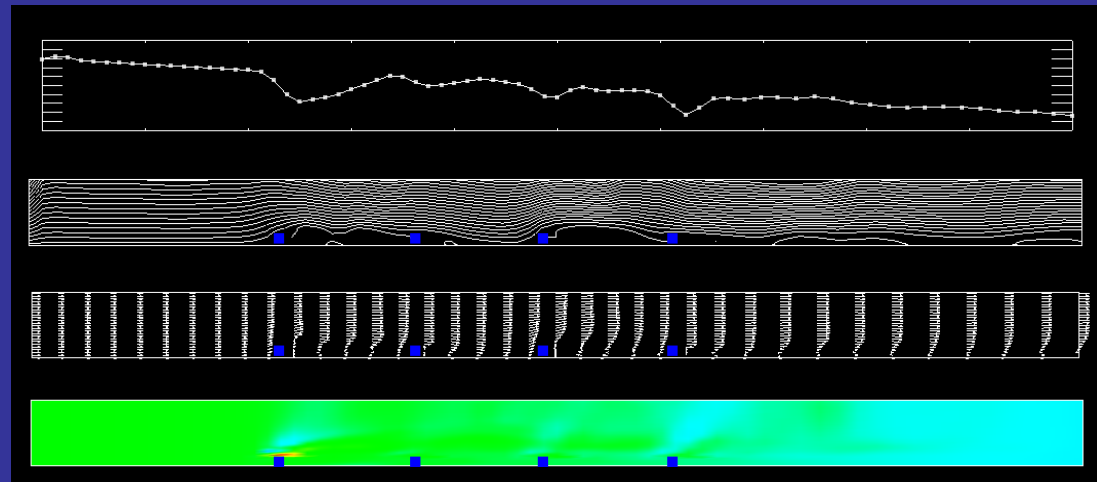
Bed elevation

Streamline

Velocity vector

$t = 0$  min.

Equilibrium

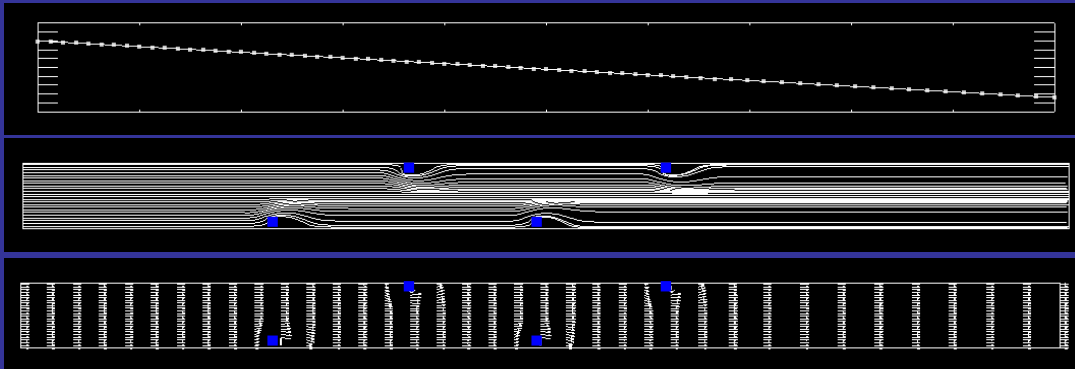


กรณีมีเขื่อนกันตลิ่งขนาดกว้าง 2.0 เมตร X หนา 0.3 เมตร โดยวางไว้ห่างเท่าๆ กัน 20.0 เมตร

# Application 2

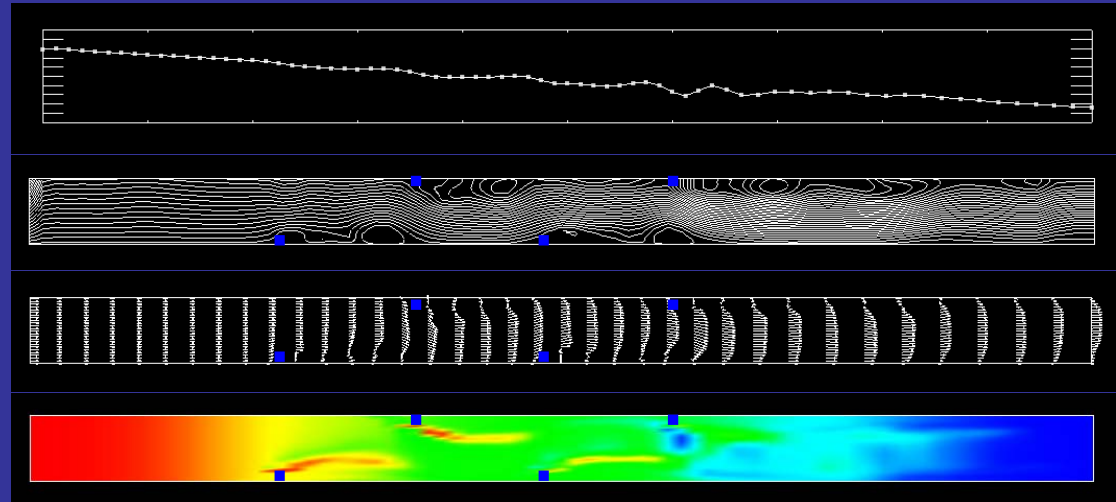
## Conditions

$$L = 80.0 \text{ m}, B = 10.0 \text{ m}, q = 50 \text{ m}^3/\text{s}, i = 1/2000, d = 1.45 \text{ mm}$$



$t = 0 \text{ min.}$

Equilibrium



กรณีมีเขื่อนกันตึ่ถึงขนาดกว้าง 2.0 เมตร X หนา 0.3 เมตร โดยวางสตั้บด้านห่างเท่าๆ กัน 20.0 เมตร



# New Conceptual Design of Spur Dike



# Spur Dike



# Natural Diversities River Methods



## Hokkaido, Japan

# Natural Diversities River Methods

Before



After



Before



After



## Hokkaido, Japan

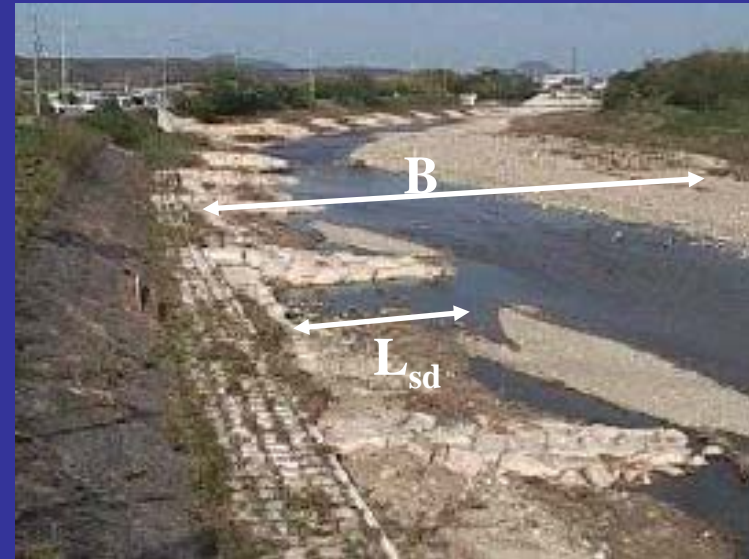
# Spur Dike Design

## Straight Channel Section

Length	$0.10B$
Height	$0.2-0.3H_{Wmax}$
Distance	$2-4L_{sd}, 10-30H_{sd}$
Side Slope	$1/20-1/100$

## Bend Channel Section

Length	$0.10B$
Height	$0.5-1.0H_{Waver}$
Distance	$>2L_{sd}$
Side Slope	$1/20-1/100$



<b>B</b>	<b>Channel width</b>
<b><math>L_{sd}</math></b>	<b>Length of spur dike</b>
<b><math>H_{Waver}</math></b>	<b>Average water depth</b>
<b><math>H_{Wmax}</math></b>	<b>Maximum water depth</b>
<b><math>H_{sd}</math></b>	<b>Height of spur dike</b>



# THE END

t= 22.0sec

